

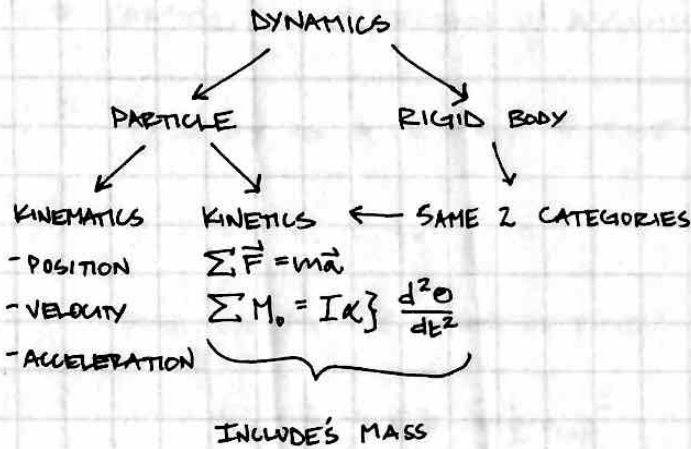
MONDAY, JAN 9 2012

HOMWORK DUE ONCE A WEEK

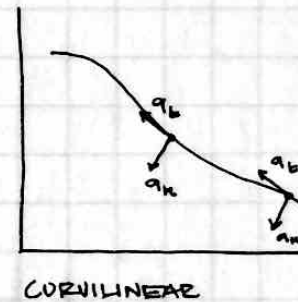
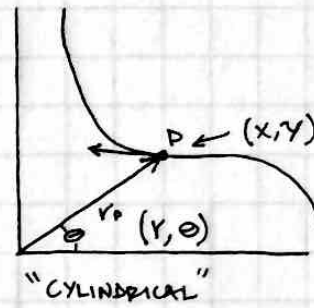
"CONSISTENTLY DO WELL ON HOMEWORK AND YOU SHOULDN'T HAVE TO WORRY ABOUT YOUR GRADE"

- CLEAR / ORGANIZED
- GIVENS / KNOWNS LIST
- FREE-BODY DIAGRAMS

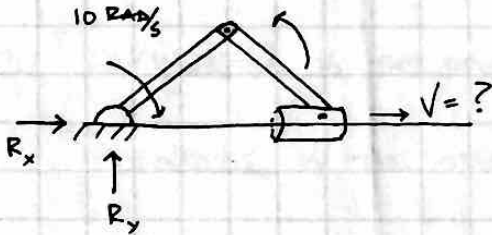
NOTES:



COORDINATE SYSTEMS:



RIGID BODY DYNAMICS



KINETICS:

- 1.) $F = ma$
- 2.) KE, PE
- 3.) IMPULSE / MOMENTUM

HOMWORK WILL BE POSTED 1/9/2012

DYNAMICS NOTES (READING)

RECTILINEAR KINEMATICS:

STRAIGHT LINE PATH - s = POSITION VARIABLE

$$v = \frac{ds}{dt} \quad a = \frac{dv}{dt} \quad \text{OR} \quad a = \frac{d^2s}{dt^2}$$

THE 3 KINEMATICS EQUATIONS:

* CONSTANT ACCELERATION IS ASSUMED *

VELOCITY AS A FUNCTION OF TIME:

$$v = v_0 + a_c t$$

POSITION AS A FUNCTION OF TIME:

$$s = s_0 + v_0 t + \frac{1}{2} a_c t^2$$

VELOCITY AS A FUNCTION OF POSITION:

$$v^2 = v_0^2 + 2a_c(s - s_0)$$

KINEMATICS IS THE STUDY OF THE GEOMETRY OF MOTION

KINETICS IS THE STUDY OF THE FORCES THAT CAUSE THE MOTION

"A PARTICLE CAN HAVE AN ACCELERATION AND A ZERO VELOCITY"

- ONLY BRIEFLY HOWEVER

BY RELATING $v = \frac{ds}{dt}$ AND $a = \frac{dv}{dt}$ THROUGH A SEPARATION OF VARIABLES,

WE GET:

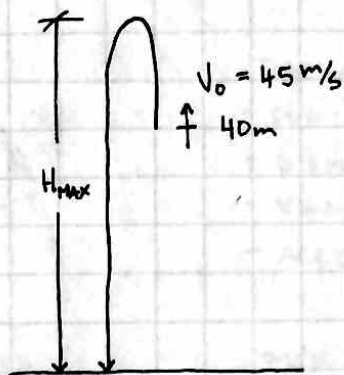
$a ds = v dv$ WHICH POST-INTEGRATION GIVES

$$\frac{v^2}{2} = \int a ds$$

JANUARY 11, 2012

RECTILINEAR POSITION, VELOCITY, ACCELERATION. CONSTANT AND VARYING ACCELERATIONS

HW FORMAT:



SMALL PROJECTILE FIRED:

$$v_0 = 60 \text{ m/s}$$
$$a = (-0.4v^3) \text{ m/s}^2$$

$$a = \frac{dv}{dt} \Rightarrow -0.4v^3 = \frac{dv}{dt} \Rightarrow \int_0^4 dt = \frac{1}{-0.4} \int_{60}^{v_f} v^{-3} dv$$

JANUARY 17, 2012 RECTILINEAR MOTION (READING NOTES)

WHEN A PARTICLE HAS ERATIC OR CHANGING MOTION, THEN ITS POSITION, VELOCITY, AND ACCELERATION CANNOT BE DESCRIBED BY A SINGLE CONTINUOUS MATHEMATICAL FUNCTION. THE MOTION MUST BE DESCRIBED BY MULTIPLE FUNCTIONS, WHICH CAN BE EASIER DEALT W/ USING GRAPHS.

FORMULA'S:

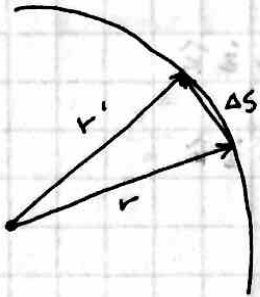
$$V = \frac{ds}{dt} ; \text{ VELOCITY} = \text{SLOPE OF S-T GRAPH}$$

JANUARY 23, 2012

HW. 3 ASSIGNMENT, DUE FRIDAY

OFFICE HOURS CHANGED

LECTURE 5 - CURVILINEAR MOTION

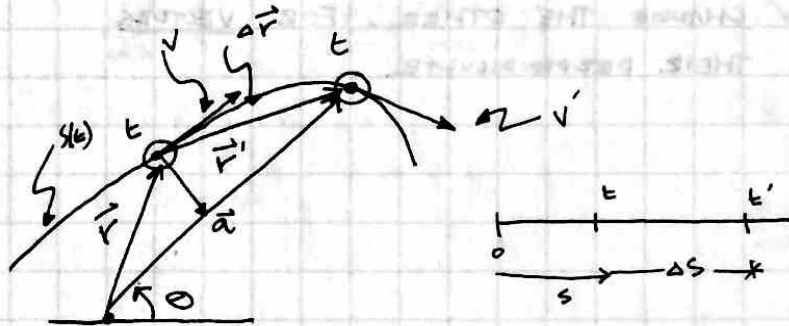


THINGS WE NEED TO BE ABLE TO FIND:

- POSITION
- DISPLACEMENT
- VELOCITY
- ACCELERATION

$$\frac{\Delta \vec{r}}{\Delta t} = \frac{d\vec{r}}{dt}$$

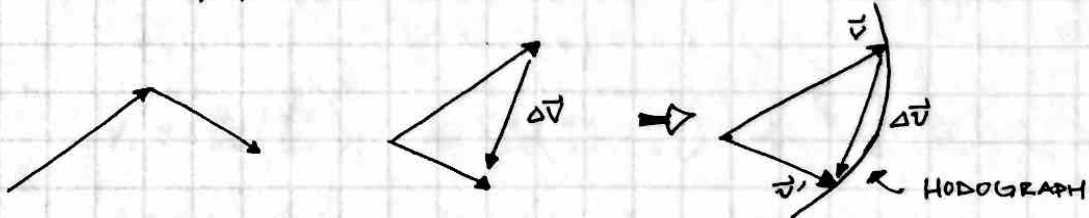
PICK ORIGIN, ARBITRARILY



$$\Delta \vec{r} = \vec{r}' + \vec{r}$$

$$\frac{\text{CHANGE IN DISPLACEMENT}}{\text{CHANGE IN TIME}} = \vec{v}_{\text{AVE}} \Rightarrow \vec{v} = \frac{d\vec{r}}{dt}$$

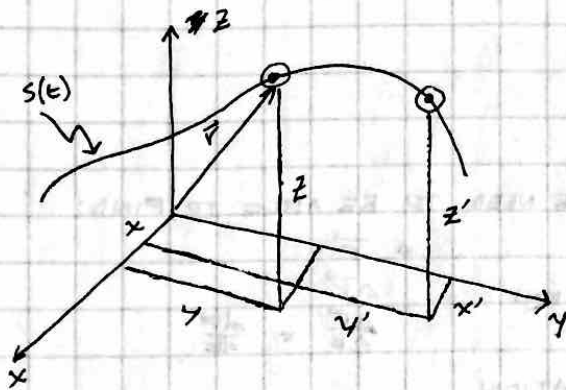
$$\text{SPEED} = |\vec{v}| = \frac{ds}{dt}$$



\vec{v} TANGENT TO $s(t)$

\vec{a} TANGENT TO HODOGRAPH

JANUARY 23, 2012, CONT.



$$\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$$

$$\vec{v} = \dot{x}\hat{i} + \dot{y}\hat{j} + \dot{z}\hat{k}$$

$$\vec{a} = \ddot{x}\hat{i} + \ddot{y}\hat{j} + \ddot{z}\hat{k}$$

ORTHOGONAL: TWO DIFFERENT VARIABLES — ONE CHANGES DOES NOT AUTOMATICALLY CHANGE THE OTHER. FOR VECTORS THAT MEANS THEIR PERPENDICULAR.

JANUARY 25, 2012

STEPHEN SILLS (HW GRADER)
SILLS @ ONID

ALWAYS STATE KNOWNS / UNKNOWN

EXAMPLE:

$$\frac{x^2}{4} + y^2 = 1$$

$$\vec{v} = \dot{x} \hat{i} + \dot{y} \hat{j}$$

$$|\vec{v}| = \sqrt{(\dot{x})^2 + (\dot{y})^2}$$

$$\frac{dy}{dx} \neq \frac{dy}{dt} = \left(\frac{dy}{dx}\right) \frac{dx}{dt}$$

$$x^2 + 4y^2 = 4$$

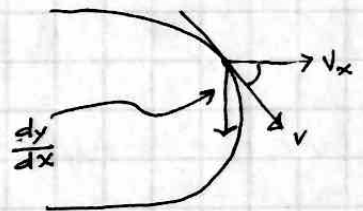
$$2x \frac{dx}{dt} + 8y \frac{dy}{dt} = 0$$

$$\frac{dy}{dx} = -\frac{x}{4y}$$

$$\frac{dx}{dt} = 10$$

$$\frac{dy}{dt} = \frac{dy}{dx} \frac{dx}{dt} = (-0.289)(10) = -2.89 \text{ m/s}$$

$$v_x = \frac{dx}{dt}; \quad v_y = \frac{dy}{dt}$$



$$a = \ddot{x} \hat{i} + \ddot{y} \hat{j} \quad a_x = 0 \Rightarrow a = a_y$$

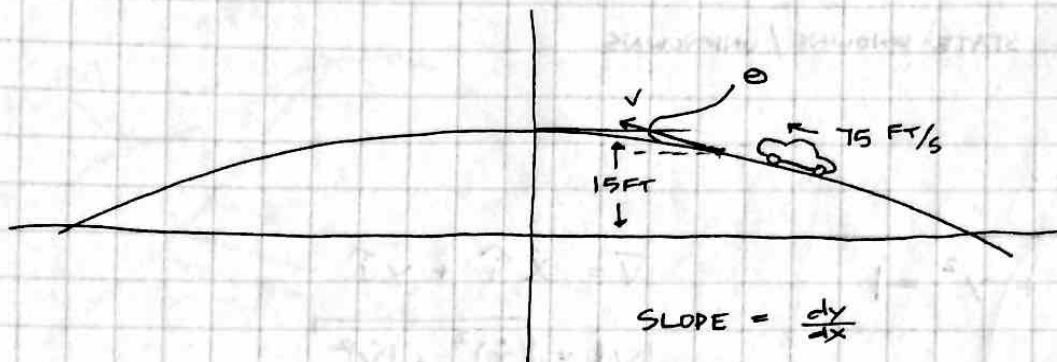
$$\ddot{y} = \frac{d}{dt} \left(\frac{dy}{dt} \right) \Rightarrow \frac{d}{dt} \left(\frac{dy}{dx} \cdot \frac{dx}{dt} \right) \Rightarrow \frac{d}{dt} \left(\frac{dy}{dx} \right) \cdot \frac{dx}{dt} + \frac{d}{dt} \left(\frac{dx}{dt} \right) \frac{dy}{dx}$$

$$\frac{d}{dt} \left(\frac{dy}{dx} \right) \cdot \frac{dx}{dt} = 10 \frac{d}{dt} \left(-\frac{x}{4y} \right) = \left(\frac{10}{4} \right) \frac{d}{dt} (x \cdot y^{-1})$$

$$= 2.5 \left[\frac{dx}{dt} (y^{-1}) \dots \right]$$

EXAMPLE

12.79



(CAN) SOLVE FOR θ

$$a = [a_x, a_y]$$

$$a = \left[\frac{d^2x}{dt^2}, \frac{d^2y}{dt^2} \right]$$

JANUARY 27, 2012

MOTION OF A PROJECTILE

CONSTANT ACCELERATION DOWNWARD

WORK EXAMPLE 12.12, 12.90

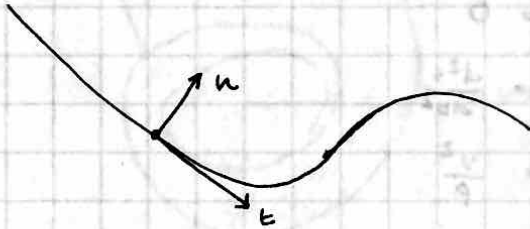
LOOK FOR HW

* TEST ON MONDAY / 6

JANUARY 30, 2012

COORDINATE SYSTEMS: n - t , r - θ

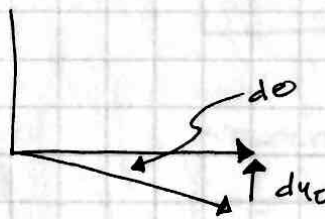
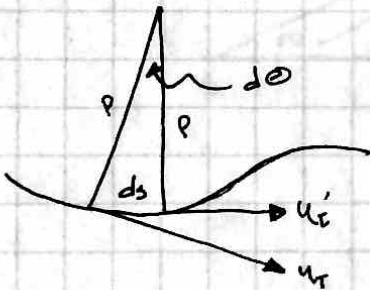
n - t , MOVES w/ PARTICLE (NORMAL - TANGENT) - TANGENT TO CURVE



DISPLACEMENT: ds

IN n - t , VELOCITY HAS NO NORMAL COMPONENT

$$\vec{a} = \frac{d}{dt}(\vec{v}) = \frac{d}{dt}(v \cdot \vec{u}_t) = \frac{dv}{dt} \vec{u}_t + \frac{dv_t}{dt} v$$



$$\begin{aligned} s &= p\theta \\ ds &= p d\theta \\ \frac{ds}{dt} &= p \cdot \frac{d\theta}{dt} \end{aligned}$$

$$\boxed{\frac{d\theta}{dt} = \frac{v}{p}}$$

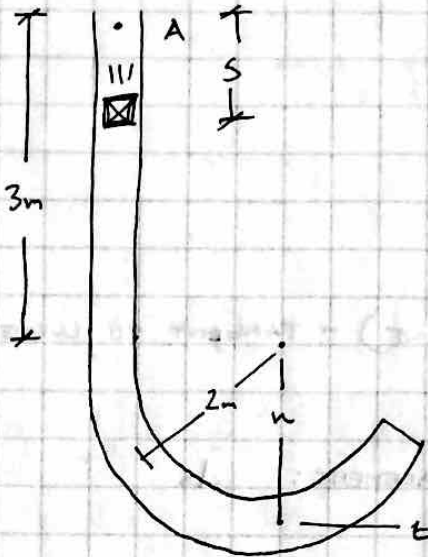
$$d(\vec{u}_\theta) = d\theta \cdot \vec{u}_n$$

ACCELERATION:

$$\vec{a} = a_t \cdot \vec{u}_T + a_n \cdot \vec{u}_n$$

$$a_t \cdot ds = v \cdot dv$$

$$a_n = \frac{v^2}{\rho}$$



$$a_t = 0.2t \text{ m/s}^2$$

v_n MUST BE ZERO

$$v_t = \frac{d\odot}{dt}$$

$$v_n = 0$$

$$a_t = \frac{d^2s}{dt^2}$$

$$a_n = \frac{v^2}{\rho}$$

PHYSICS CHALLENGE

DYNAMICS # 4

DYNAMICS # 5

ENGE 202

MASTERING PHYSICS

MATH

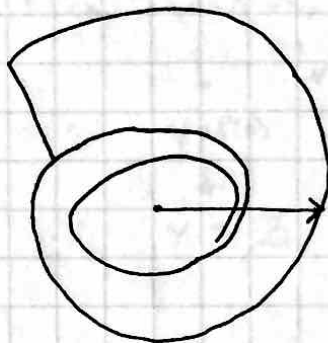
JANUARY FEBRUARY 1, 2012

POLAR / CYLINDRICAL COORDINATES



$$r = C \cdot \theta$$

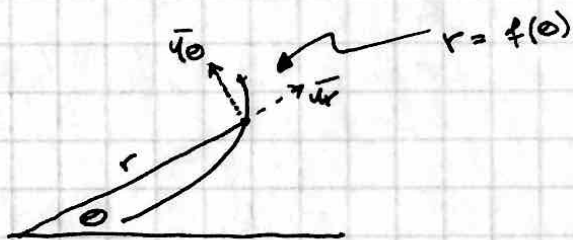
ARCHIMIDES PRINCIPLE



$$r = a \cdot e^{b\theta}$$

← DEFINES A CURVE THAT IF YOU PASS WATER THROUGH, IT WOULD EXPERIENCE THE LEAST AMOUNT OF RESISTANCE.

NOTES:



POSITION:

$$\vec{r} = r \cdot \vec{u}_r$$

VELOCITY:

$$\vec{v} = \frac{d\vec{r}}{dt} = \frac{d}{dt}(r \cdot \vec{u}_r)$$

$$= \frac{dr}{dt} \vec{u}_r + r \frac{d\vec{u}_r}{dt}$$

ACCELERATION:

$$\vec{a} = a_r \vec{u}_r + a_\theta \cdot \vec{u}_\theta$$

FEBRUARY 3, 2012

TEST MATERIAL:

- RECTILINEAR MOTION
- ERRATIC MOTION

WHEN COMPUTING VELOCITY, ALWAYS 'FINISH' PROBLEM BY PLUGGING IN v_x AND v_y TO SQUARE ROOT

- GRAPHS OF $r(t)$, $v(t)$, $a(t)$
- SPECIFICALLY $a(s) \rightarrow v(s)$, VICE VERSA

12-57

12-58

CURVILINEAR:

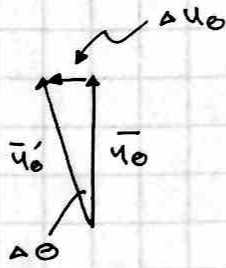
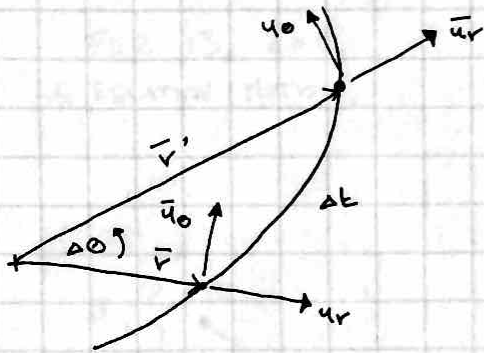
$$\dot{y} = \frac{dy}{dt} = \left(\frac{dy}{dx} \right) \left(\frac{dx}{dt} \right)$$

↓ ↓

$y = f(x)$ \dot{x} (GIVEN)

↓

$$\dot{y} = \frac{dy}{dx}$$



$$\bar{u}'_0 = \bar{u}_0 + \Delta \bar{u}_0$$

$$\Delta \bar{u}_0 = \bar{u}'_0 - \bar{u}_0$$

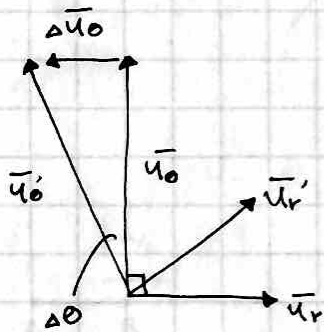
$$\Delta u_0 = |\Delta \bar{u}_0|$$

$$= |\bar{u}_0| \times \Delta \theta$$

$$= 1 \cdot \Delta \theta = \Delta \theta$$

$$\boxed{\Delta u_0 = \Delta \theta}$$

$$\frac{d}{d\theta}(\bar{u}_0) = \lim_{\Delta \theta \rightarrow 0} \frac{\Delta \bar{u}_0}{\Delta \theta} = -\bar{u}_r$$

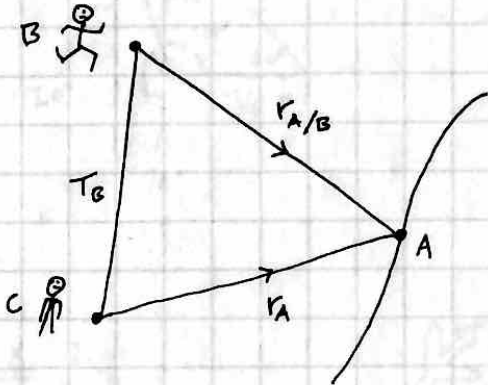


FEB, 8 2012

DEPENDENT MOTION

FEB 13, 2012

* RELATIVE MOTION

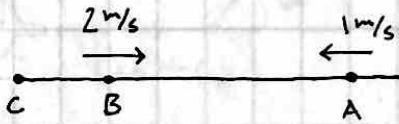


$$r_A = r_B + r_{A/B}$$

$$r_{A/B} = r_A - r_B$$

$$v_{A/B} = v_A - v_B$$

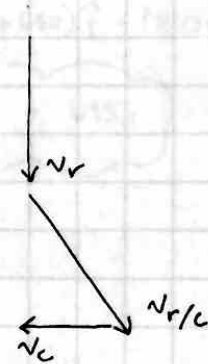
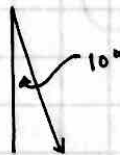
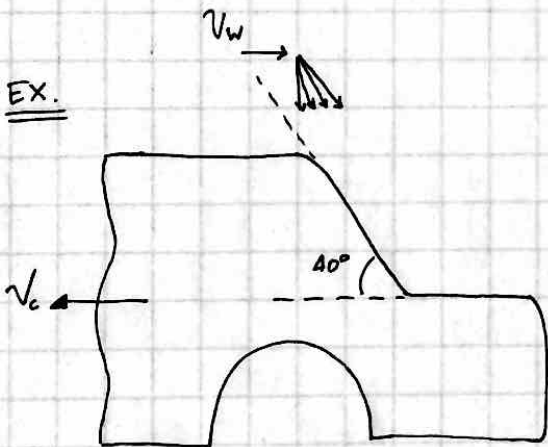
$$a_{A/B} = a_A - a_B$$



$$v_{A/B} = (-1) - (+2) = \underline{\underline{-3}}$$

$$v_{B/A} = -v_{A/B}$$

EX.



$$v_{r/c} = v_r - v_c$$

$$v_{r/c} = v_r - v_c$$

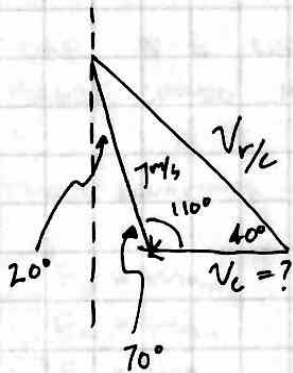
$$v_r = v_c + v_{r/c}$$

MUST MAINTAIN!

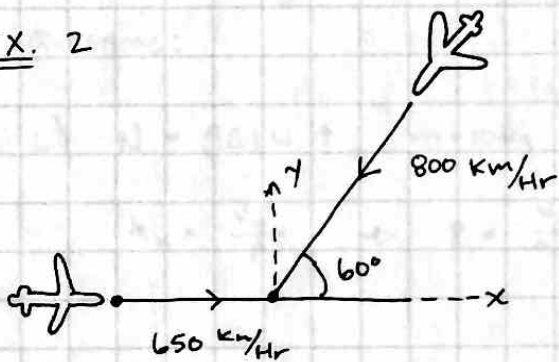
FEBRUARY 13, 2012

EX. TAKE 2

20° ANGLE



EX. 2



$$\vec{V}_B = -800 \cos(60^\circ) \hat{i} - 800 \sin(60^\circ) \hat{j}$$

$$\vec{V}_A = 650 \hat{i}$$

$$\vec{V}_{B/A} = \vec{V}_B - \vec{V}_A$$

$$= (-400 + 650) \hat{i} - (800 \sin(60^\circ)) \hat{j}$$

$$= 250 \hat{i} - 693 \hat{j}$$

FEB 17, 2012

NORMAL AND TANGENTIAL EQUATIONS OF MOTION

- NORMAL COMPONENT OF FORCE IS ALWAYS ~~FORWARD~~ POINTED TOWARDS THE CENTER OF CIRCLE

- USE N-E COORDINATED WHEN PARTICLE IS MOVING ALONG A KNOWN CURVED PATH

THREE EQUATIONS OF MOTION:

$$\begin{aligned}\sum F_t &= ma_t \\ \sum F_n &= ma_n \\ \sum F_g &= ma_g\end{aligned}$$

QUESTIONS:

1.) $N = 98.1 \text{ N } \uparrow$, $m = 10 \text{ kg}$, $v_b = 2 \text{ m/s}$

$$a_n = \frac{v_b^2}{r} \rightarrow r = \frac{v_b^2}{a_n}, \quad r = 0.4 \text{ m } \quad \times$$

2.) $F_n = F_g = mg = 20 \text{ lb}$

$$a_n = \frac{v_b^2}{r} \quad v_b = (a_n r)^{1/2} \Rightarrow v_b = [(10/32.2)(7)]^{1/2} =$$

FEBRUARY

* HW

13.1, 13.4, 13.5, 13.6, 13.12, 13.26, 13.88, 13.89
CAN BE TURNED IN FRIDAY

* CYLINDRICAL COORDINATES

$$v_r = \frac{dr}{dt} = \dot{r}$$

$$v_\theta = r\dot{\theta} =$$

$$a_r = \ddot{r} - r\dot{\theta}^2$$

$$a_\theta = r\ddot{\theta} + 2\dot{r}\dot{\theta}$$

* LOOK AT FIGURE 13.7 IN BOOK

- STUDY EXAMPLES
- FUNDAMENTAL PROBLEMS
- 13.10, 13.11 (EXAMPLES)

FEBRUARY 22, 2012

MOMENT OF INERTIA

TEST:

- REVIEW HOMEWORKS (SINCE TEST 1)
- FUNDAMENTAL PROBLEMS
- RELATIVE MOTION
- PULLEY PROBLEMS

12.9, 12.10, 13.1-13.6

- RELATIVE MOTIONS, LOM IN CARTESIAN (FROM HW 1!)
- ALLOWED ONE NOTESHEET (1 PAGE)

LINEAR

s
 $v = \dot{s}$
 $a = \ddot{s} = \dot{v}$
 F
 m

ROTATIONAL

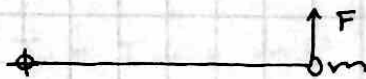
θ
 $\omega = \dot{\theta}$
 $\alpha = \dot{\omega} = \ddot{\theta}$
 τ
 $I = mr^2$

RELATION

$s = r\theta$
 $v = r\omega$
 $a = r\alpha$
 $\tau = Fr$
 $I = mr^2$

N-E SYSTEM:

$$a_E = \dot{v}, \quad a_n = \frac{v^2}{r}$$

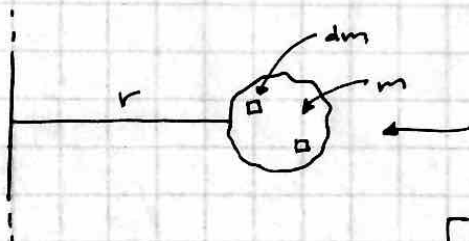


$$F = m \cdot a$$

$$F_E = m \cdot a_E = m \dot{v} = m r \dot{\omega}$$

$$\tau = F_E \cdot r = m r^2 \dot{\omega} = m r^2 \alpha$$

$$\tau = (m r^2) \alpha$$



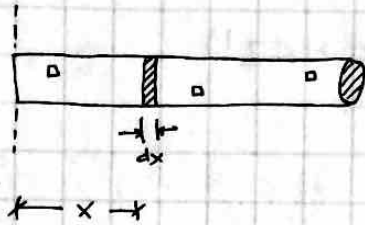
PARTS OF THE MASS ARE AT FURTHER DISTANCES

$$I = \int dI = \int r^2 dm$$

FEB 22, 2012

TRANSLATE $I = \int_{\text{DOMAIN}} r^2 dm \rightarrow I = mK^2$

$$R = \sqrt{\frac{I}{M}} \Rightarrow R = \sqrt{\frac{\int r^2 dm}{M}}$$



LENGTH = x

VOLUME:

$$dV = A dx$$

$$dm = \rho dV = \rho A dx$$

$$dI = dm x^2, \text{ so:}$$

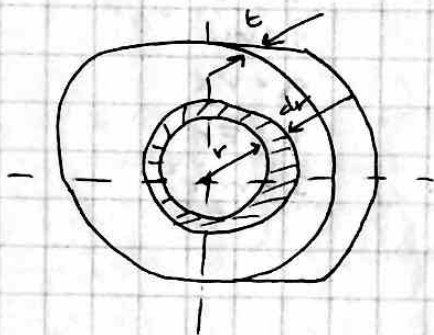
$$dI = \rho A x^2 dx$$

$$I = \rho A \int_0^L x^2 dx$$

$$= \rho A \frac{L^3}{3}$$

$$= (\rho A L) \frac{L^2}{3}$$

$$I = \frac{mL^2}{3}$$

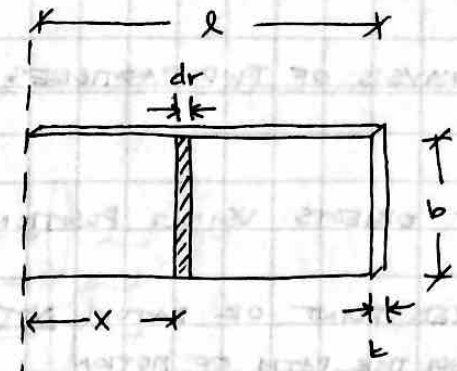


$$dI = r^2 dm$$
$$= 2\pi t r^3 dr$$

$$I = 2\pi t \rho \frac{R^4}{4}$$

$$= (\pi r^2) t \rho = \frac{mR^2}{2}$$

$$= \frac{mR^2}{2}$$



$$V = lbt$$

$$dm = \rho dV = A dx$$

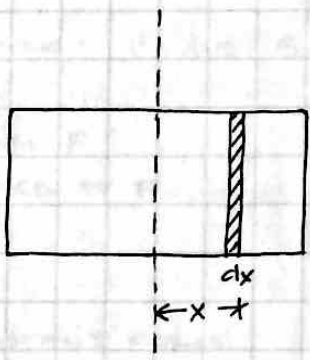
$$I = \frac{mL^2}{3}$$

SAME AS BAR ABOUT
END

$$\underbrace{\rho t b dx}_m \Rightarrow dI = x^2 \rho t b dx$$

$$I = \rho t b \left[\frac{x^3}{3} \right]_0^L$$

$$I = \rho t b \left[\frac{L^3}{3} \right]$$



$$dA = b \cdot dx$$

$$dV = b t dx$$

$$dm = \rho b t dx$$

$$dI = x^2 dm = x^2 \rho b t dx$$

$$I = \rho b t \frac{1}{3} [$$

$$I = \frac{ML^2}{3}$$

PARALLEL AXIS THEOREM

KNOW HOW TO COMPUTE MOI

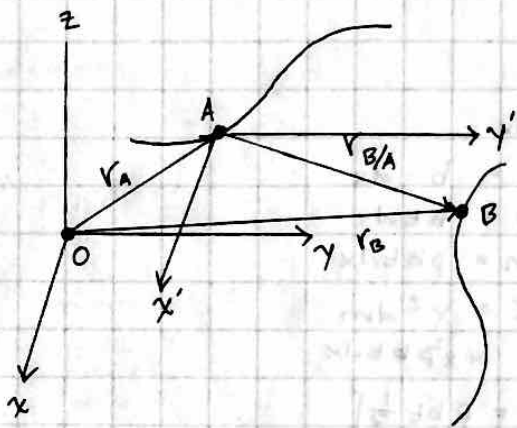
$$I_d = I_{cm} + md^2$$

NOTES, CHAPTER 12.9 READING

* ABSOLUTE DEPENDENT MOTION ANALYSIS OF TWO PARTICLES

- SPECIFY LOCATION OF DEPENDENT OBJECTS USING POSITION COORDINATES.
- MUST BE MEASURED FROM A FIXED POINT OR DATUM, NOT NECESSARILY THE SAME, BUT ALONG THE PATH OF MOTION

* RELATIVE MOTION OF TWO PARTICLES USING TRANSLATING AXES



POSITION:

$$r_B = r_A + r_{B/A}$$

VELOCITY:

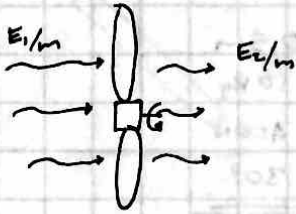
$$v_B = v_A + v_{B/A}$$

ACCELERATION:

$$a_B = a_A + a_{B/A}$$

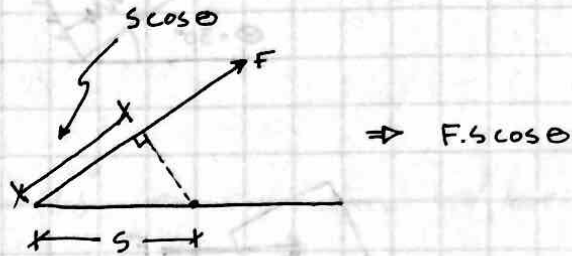
FEBRUARY 27, 2012

* WORK AND ENERGY



WORK:

$$W = \vec{F} \cdot \vec{s} = F s \cos \theta$$

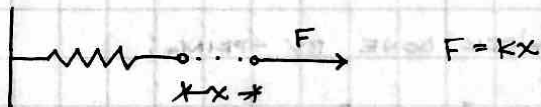


* POSITIVE WORK: F AND S ARE IN SAME DIRECTION

(+) ALONG F

(-) OPPOSED TO F

* NON-CONSTANT FORCE



~~X~~ $x \dots F$
 $x + dx \dots F + dF \Rightarrow dW \Rightarrow Fx + Fdx + x dF + dF dx$

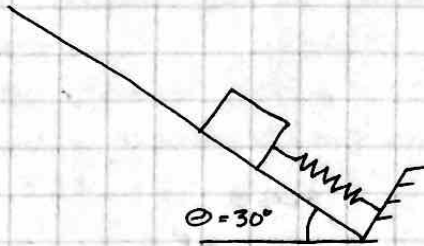
$dW = (F + dF)(dx) \Rightarrow Fdx + dF dx \Rightarrow Fdx \Rightarrow F = kx$

$$W = k \int_{x_1}^{x_2} x dx \Rightarrow \frac{kx_2^2}{2} - \frac{kx_1^2}{2} \quad \boxed{W = \frac{kx_2^2}{2} - \frac{kx_1^2}{2}}$$

- MUST PAY ATTENTION TO INITIAL DISPLACEMENT WITH SPRINGS.

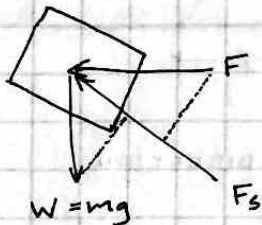
2/27/2012 CONT.

EX:



$$\begin{aligned} s_1 &= 0.5 \text{ m} \\ m &= 10 \text{ kg} \\ F &= 400 \text{ N} \\ \theta &= 30^\circ \end{aligned}$$

$$\begin{aligned} W &= ? \\ \Delta s &= 2 \text{ m} \end{aligned}$$



WORK DONE BY F :

$$\begin{aligned} &(F \cos(30))(2 \text{ m}) \\ &= 400 \cos(30) \text{ N} \cdot 2 \text{ m} = 692.8 \text{ J} \end{aligned}$$

WORK DONE BY mg

$$\begin{aligned} W &= -(mgs \sin \theta) \cdot s \\ &= (10)(9.81)(0.5) \Rightarrow -98.1 \end{aligned}$$

WORK DONE BY SPRING:

$$\frac{kx_2^2}{2} - \frac{kx_1^2}{2} \Rightarrow -90 \text{ J}$$

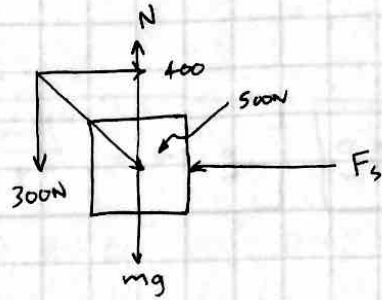
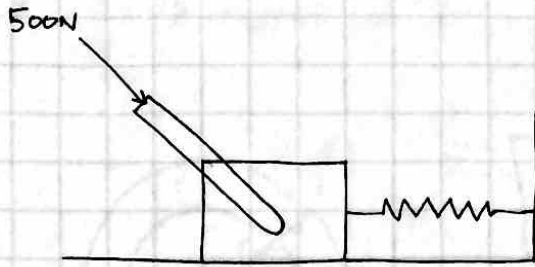
TOTAL WORK:

$$\sum W \Rightarrow (692.8 - 98.1 - 90) \text{ J}$$

* NOTE *

IF SPRING WERE LET TO OSCILLATE,
IT WOULD OSCILLATE AROUND
LOADED EQUILIBRIUM.

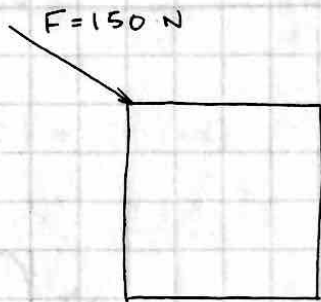
2/29/2012



$$\sum F_x = 400N - kx$$

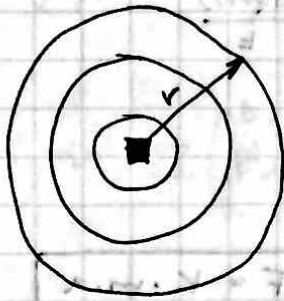
$$\frac{400N - 500x}{10} \Rightarrow "a = f(s)" \Rightarrow \text{INTEGRATE TO GET } v$$

Ex.



$$\sum F_x: 150 \cos(\theta)$$

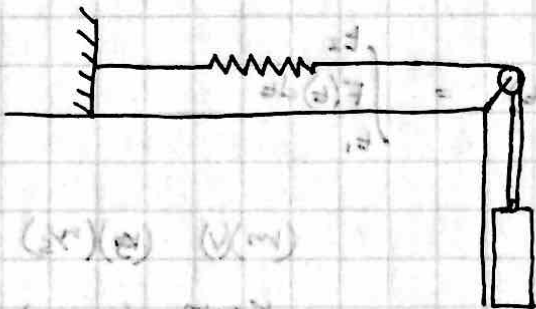
7/7 3/2/2012



$$F_g = G \frac{mM}{r^2} = m \cdot g$$

$$g = \frac{GM}{r^2}$$

Ex.

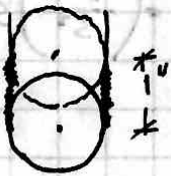


$$W_s = \frac{1}{2} k (x_2^2 - x_1^2)$$

$$F_{s1} = 60N$$

$$k_s = 300 N/m$$

$$x_1 = \frac{F_{s1}}{k} = \frac{60N}{300N/m} = \underline{\underline{0.2m}}$$



$$W_g = mg(\Delta h) = (50kg)(9.81m/s^2)(0.2m)$$

$$W_g = 981 N$$

PULLEY MOVES 1" FOR EVERY 2" OF ROPE DISPLACED

3/5/2012

v_1, v_2, t

$$a = \frac{v_2 - v_1}{t} \Rightarrow ma = \frac{mv_2 - mv_1}{t} = \frac{\Delta(mv)}{t}$$

= RATE OF CHANGE OF MOMENTUM

$$F \propto \frac{\Delta mv}{t} \Rightarrow F = \frac{m(v_2 - v_1)}{t} \Rightarrow \boxed{F = k \cdot m \cdot a}$$

\uparrow 1N \uparrow 1kg \uparrow 1m/s²
So k MUST BE 1

$$m \cdot v = I = \int F \cdot dt = F(\Delta t) = \int_{t_1}^{t_2} F(t) dt$$

FINAL REVIEW NEXT FRIDAY
TEST #3 NEXT WEDNESDAY

$$(m)(v) \quad (kg)(m/s)$$
$$\frac{kg \cdot m}{s} = \left(\frac{kg \cdot m}{s^2} \right) s$$

IMPULSE IS A NON-CONSERVATIVE FORCE
(DIFFERENT THAN ENERGY)

CHAPTER 15

IMPULSE AND MOMENTUM:

$$\sum \vec{F} = m\vec{a} = m \frac{d\vec{v}}{dt} \Rightarrow \sum \int_{t_1}^{t_2} \vec{F} dt = m \int_{v_1}^{v_2} dv$$

$$\Rightarrow \sum \int_{t_1}^{t_2} \vec{F} dt = mv_2 - mv_1$$

$$\Rightarrow \boxed{mv_1 + \sum \int_{t_1}^{t_2} \vec{F} dt = mv_2}$$

* PRINCIPLE OF LINEAR
IMPULSE AND MOMENTUM *

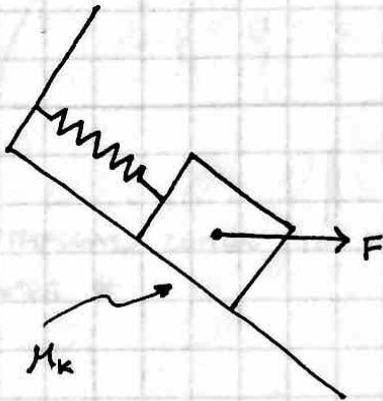
3/12/2012

DYNAMICS REVIEW:

TEST: ALL 14, 15.1, 2, 3. 2/3 PROBLEM

- SPRING
 - GRAVITY
 - FORCE
- } PROBLEMS

PROFESSOR RECOMMENDED STARING
DOWN BARREL OF GUN...



FIND VELOCITY AT $t = 1s$

* ANGLE OF REPOSE