

ME 383 1/8/2012

HOMEWORK NOT COLLECTED
QUIZES ON THURSDAYS

HOMEWORK DUE THURSDAYS:

- PROBLEMS ON WEBSITE
- SPOON TEST: 1ST/2ND CHOICE
- READ F.S. APPENDIX ONLINE OR IN BOOK (ULLMAN)

* KEY POINTS OF COURSE:

- FIND FORCES EXTERNAL TO ASSEMBLY (SCENARIO'S)
- ESTIMATE DESIGN FACTOR OF SAFETY
- FIND FORCES ON PARTS
- DETERMINE CRITICAL LOCATIONS
- DETERMINE MATERIAL PROPERTIES AND GEOMETRY AT CRITICAL LOCATIONS
- FIND STRESS / STRAIN AT C.L.
- APPLY FAILURE THEORY AND CALCULATE F.S.
- COMPARE DESIGN F.S. TO CALCULATED
- DETERMINE WHAT TO DO NEXT
- APPLY OR ALL OF ABOVE TO MACHINE COMPONENTS

ALL TOPICS FOR EXAMS

EXAM 1 THROUGH STATIC FAILURE THEORIES

* FAILURES FOR HELICOPTER PARTS:

WEAR

DUCTILE RUPTURE

⋮

"CLASSICAL"

$$FS = FS_{\text{MATERIAL}} \cdot FS_{\text{STRESS}} \cdot FS_{\text{GEO}} \cdot FS_{\text{FAILURE THEORY}} \cdot FS_{\text{RELIABILITY}}$$

- ↓
- 1.0 (KNOWN)
 - 1.1 (HANDBOOK VALUES)
 - 1.2 (NOT KNOWN)

$FS_{\text{STRESS}} \rightarrow$ 1.0 - 1.1 (LOAD WELL DEFINED)
1.2 - 1.3 (AVERAGE)
1.4 (??)

$FS_{\text{GEO}} \rightarrow$ 1.0 (AVE)
1.1 (DIM NOT CLOSELY HELD)

$FS_{\text{FAILURE THEORY}} \rightarrow$ 1.0 - 1.1 (GOOD)
1.2 (EXTENSION)

$FS_{\text{REL}} \rightarrow$ < 90% $FS = 1$
91-98% $FS = 1.2 - 1.3$
7/99% $FS = 1.4 - ??$

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TEAM MEETING: 10:00 AM MONDAY

* READING NOTES: CHAPTER 1:

- UNILATERAL TOLERANCE: VARIATION LIMITED TO ONLY ONE DIRECTION

IE. $1.005^{+0.004}$
 -0.000 IN

- GAP DIMENSIONS NEAR LIMITS ARE RARE, SO A STATISTICAL MEASURE IS GENERALLY USED. FOR A NORMAL DISTRIBUTION:

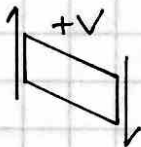
$\bar{w} = \sqrt{\sum t^2}$

A MONTE CARLO COMPUTER SIMULATION WOULD BE A BETTER FIT.

* ME 383 REVIEW NOTES:

SHEAR AND MOMENT DIAGRAMS:

- POSITIVE SHEAR ROTATES BEAM SLICE CLOCKWISE, VICE-VERSA FOR NEGATIVE



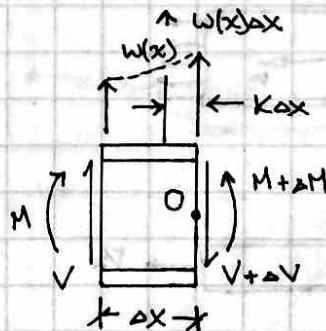
- POSITIVE MOMENT MAKES BEAM "SMILE", AND VICE-VERSA



- RELATIONSHIPS:

$\frac{dV}{dx} = w(x) \Rightarrow V = \int w(x) dx$

$\frac{dM}{dx} = V \Rightarrow M = \int V(x) dx$



$\sum F_y = 0;$

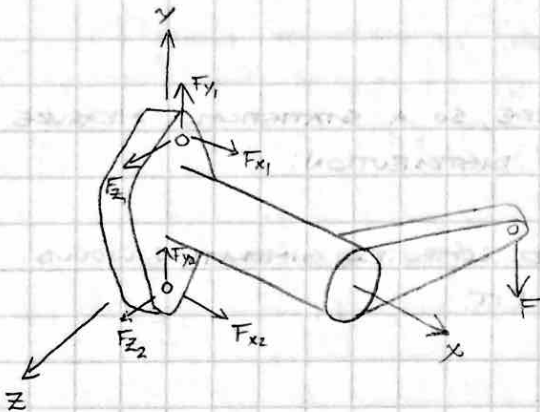
$V + w(x)dx - (V + dV) = 0$

$\Delta V = w(x) dx$

1/9/2013

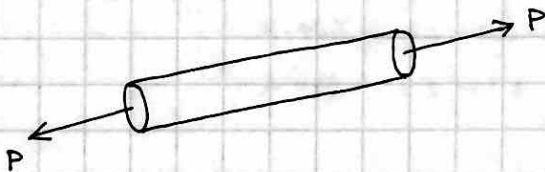
WHEN CONSTRUCTING SHEAR/MOMENT DIAGRAMS:

- ① FBD BEAM. LABEL ALL REACTIONS, IF CANTILEVER THEN REACTION MOMENT
- ② CONSTRUCT V DIAGRAM
- ③ LOCATE KEY POINTS ON V DIAGRAM; PAYING CLOSE ATTENTION TO WHERE $V=0$ IE: BENDING MOMENT ZERO
- ④ CONSTRUCT M DIAGRAM



$$\begin{aligned} \sum F_x = 0 &= F_{x1} + F_{x2} \\ \sum F_y = 0 &= F_{y1} + F_{y2} - F \\ \sum F_z = 0 &= F_{z1} + F_{z2} \\ \sum M_x = 0 &= -10F + 2.5F_{z1} - 2.5F_{z2} \\ \sum M_y = 0 & \\ \sum M_z = 0 &= -12F - 2.5F_{x1} + 2.5F_{x2} \end{aligned}$$

LECTURE NOTES:



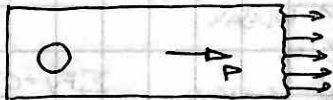
UNIAXIAL:

$$\sigma = \frac{P}{A}$$

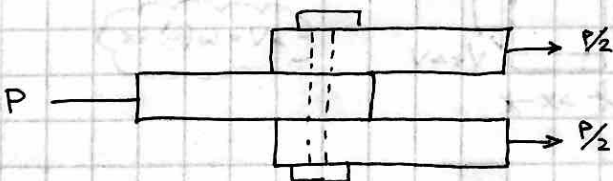
$\hookrightarrow S_y$: YIELD

S_u : ULTIMATE

S_e : ENDURANCE LIMIT

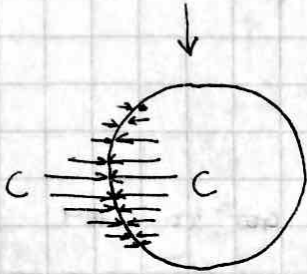
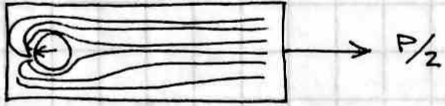


MATERIALS PROPERTIES
CHANGE IN TENSION VS.
COMPRESSION

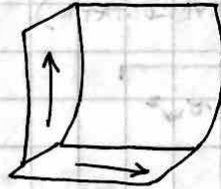
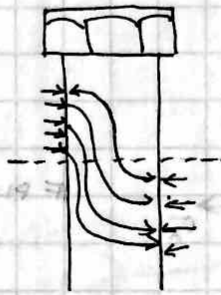
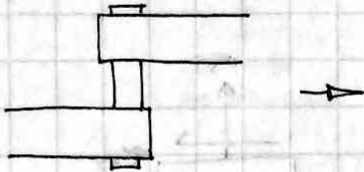


$$\tau = \frac{P/2}{A}$$

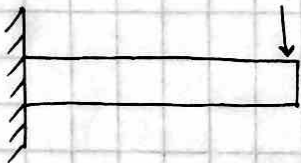
1/10/2013



"IN ORDER TO GET FROM TENSION TO COMPRESSION YOU HAVE TO GO THROUGH SHEAR"



GEAR SHOWN FAILED IN BENDING



$$\sigma = \frac{Mc}{I}$$

$$\tau = \frac{VQ}{Ib}$$

← GENERALLY NOT SIGNIFICANT

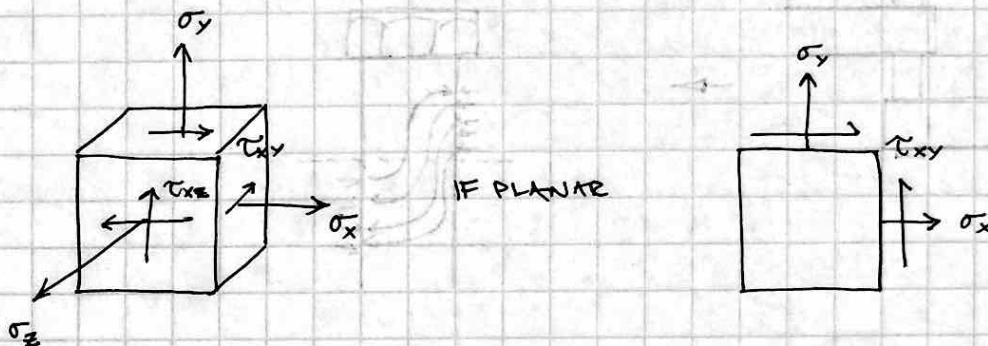
1/14/2013 TEAM MEETING NOTES:

- GOOGLE DOCS

- * QUIZ ON THURSDAY
- 2 PROBLEMS
- 1 STATE OF STRESS, 1 EQUILIBRIUM

MOHR'S CIRCLE / MANUAL S.S.

- * HW: STIFFNESS / DEFLECTION PROBLEMS — PROBABLY WON'T GET TO THEM IN LECTURE

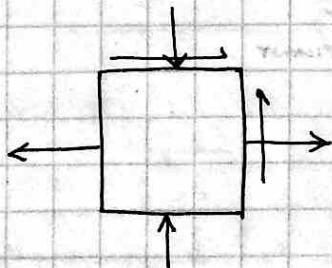


$$\sigma_{\text{AVE}} = \frac{\sigma_x + \sigma_y}{2} \text{ (HYDROSTATIC)}$$

$$\tau = \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

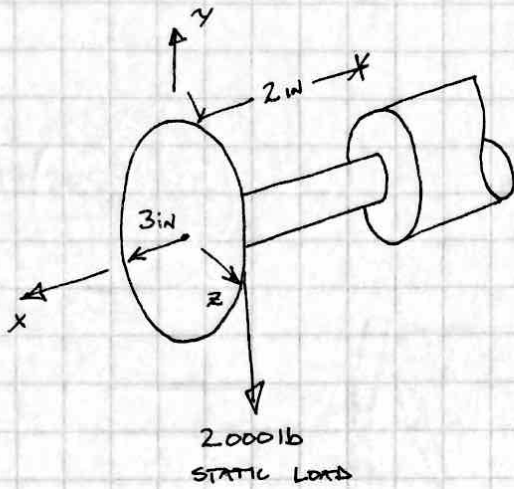
$$\tan 2\phi_p = \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$$

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$



1/15/2013

* EQUILLIBRIUM EXAMPLE:



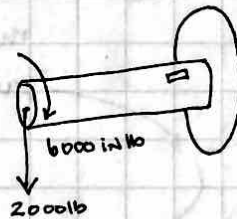
"VISUALIZE AS FLUID FLOWING"

- STRESS CONCENTRATIONS:
RIGHT-ANGLES ARE BAD

LOADS:

- BENDING, TORSIONAL

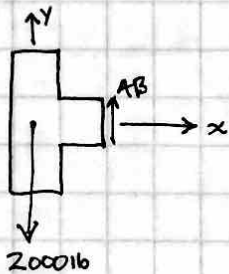
- COULD REDRAW AS →



$$A = 0.78 \text{ in}^2$$

$$I = 0.049 \text{ in}^4$$

$$J = 0.098 \text{ in}^4$$



$$\sum F_x = 0$$

$$\sum F_y = 0 = -2000 + F_{y,AB}$$

$$\sum M_z = 0 = 2 \cdot (F_y)_{AB} + (M_z)_{AB}$$

$$(M_z)_{AB} = 4000 \text{ lb}\cdot\text{in}$$

$$(F_y)_{AB} = 2000 \text{ lb}$$

$$T = M_x = 6000 \text{ in}\cdot\text{lb}$$

$$\sigma_x = \frac{M_z}{I} = \frac{4000}{0.049} = 81.63 \text{ Kpsi}$$

$$\tau_{xy} = \frac{T r}{J} = \frac{6000 \cdot 3}{0.098} = 30.6 \text{ Kpsi}$$

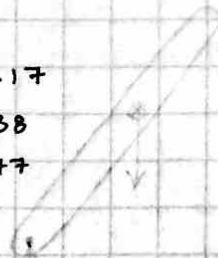
$$\sigma_y = 0;$$

$$\sigma_z = 0$$

$$\sigma_{p1} = 32.71 \quad 57.17$$

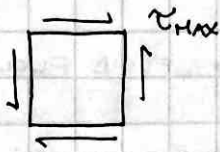
$$\sigma_{p2} = -28.63 \quad -16.38$$

$$\tau_{MAX} = 30.68 \quad 36.77$$

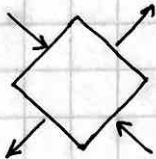


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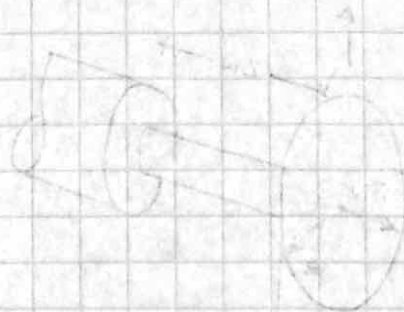
DUCTILE:



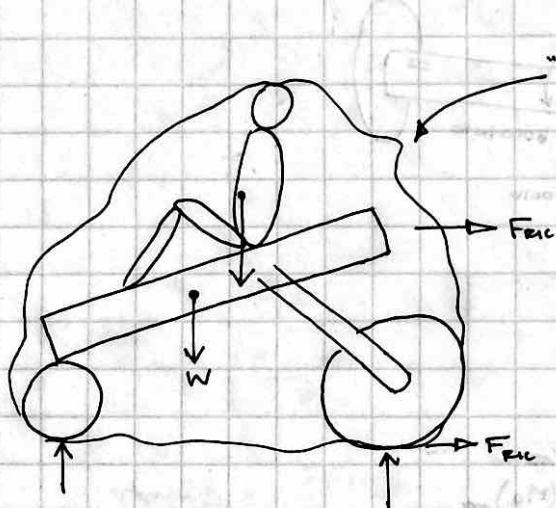
BRITTLE



$\sigma = \tau_{max}$



BIKE SWING ARM EXAMPLE



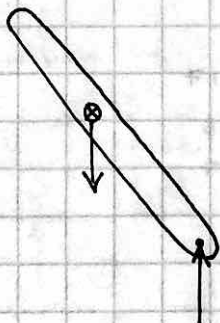
MUST GO THROUGH THE ENVELOPE

"WHAT ARE THE EXTERNAL FORCES ACTING ON BLOB?"

"REPLACE THE OBJECT WITH THE BLOB"

* KNOW FBD'S ...

-SWINGARM:

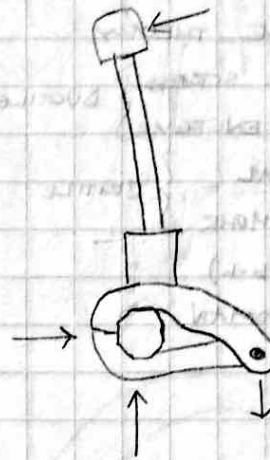
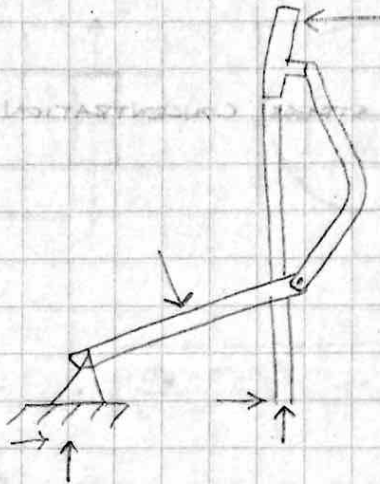


1/15/2013

LAB ASSIGNMENT #1 (2)

- ON SYLLABUS, 1 PAGE WRITE UP

1/17/2013



SURVIVABILITY - BETTER DEFINITION

1/22/2013

- HW: 5.1 a, d, e
- 5.4 b, d
- 5.19 a, c, e
- 5.36

NEW MATERIAL:

STATIC FAILURE THEORY

- MAX SHEAR STRESS } DUCTILE
- DISTORSION ENERGY } DUCTILE
- MAX NORMAL } BRITTLE
- MODIFIED MOHR } BRITTLE

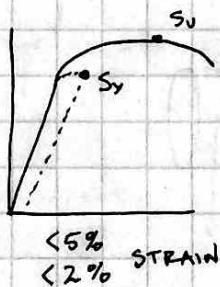
FATIGUE (TABLE b-b)

- MODIFIED GOODMAN

* STRESS CONCENTRATION FACTORS

NOTES:

~~IS IT~~ DUCTILE OR BRITTLE?



WHY MAKE SOMETHING BRITTLE?
- STRENGTH (HARDENING)

FAILURE IS EXPECTED TO OCCUR WHEN

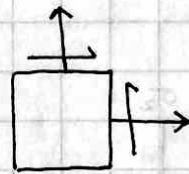
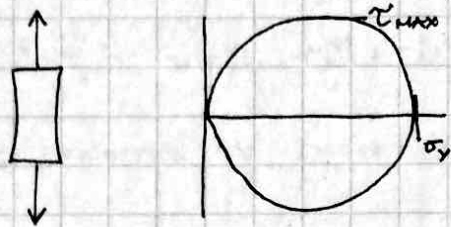
$$F.S. = n = \frac{S_y}{\sigma} \quad \begin{array}{l} \rightarrow S_y = F.S. \sigma \\ \rightarrow \sigma = \frac{S_y}{F.S.} \end{array}$$

1/22/2013

MAX SHEAR STRESS (DUCTILE)

- FAILURE PREDICTED TO OCCUR WHEN YIELDING OCCURS TO DUE MAX SHEAR EXCEEDING $\frac{S_y}{2 \cdot F.S}$

$S_{ey} (S_y), S_{eu}, S_{ev}, S_e$
 τ_{xy}



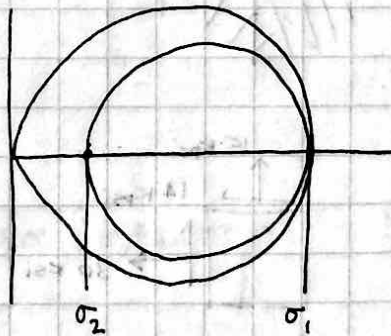
40,000 psi

$$\tau_{MAX} = \frac{40,000 \text{ psi}}{2 \cdot 4} = 5,000 \text{ psi}$$

$$\tau_{MAX} = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

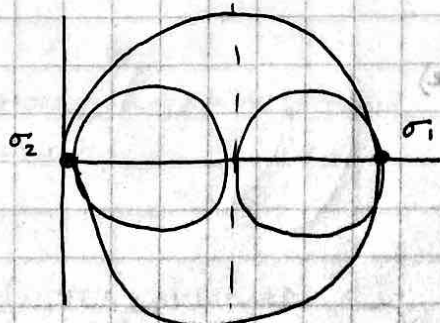
3 CASES: $\sigma_1 > \sigma_2 > 0$

1.)



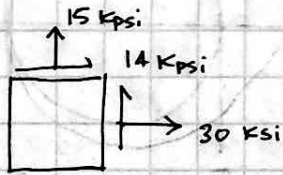
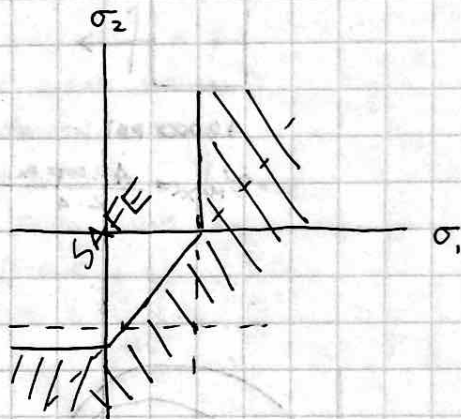
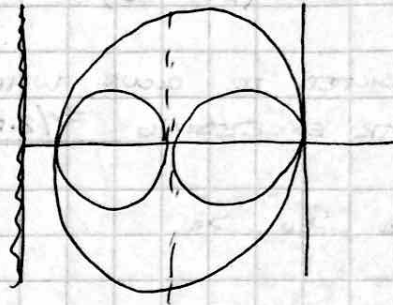
$$\tau_{MAX} = \frac{\sigma_1}{2}$$

2.) $\sigma_1 > 0 > \sigma_2$



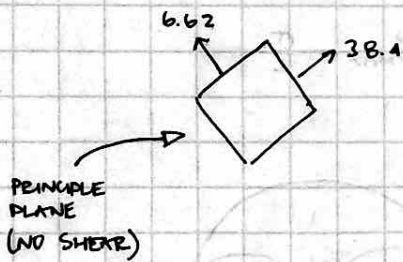
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$$\sigma_1 < \sigma_2 < 0$$



$$S_y = 57 \text{ Kpsi}$$
$$F.S. = ?$$

$$\sigma_1 = 38.4 \text{ Kpsi}$$
$$\sigma_2 = 6.62 \text{ Kpsi}$$
$$\sigma_3 = 0$$

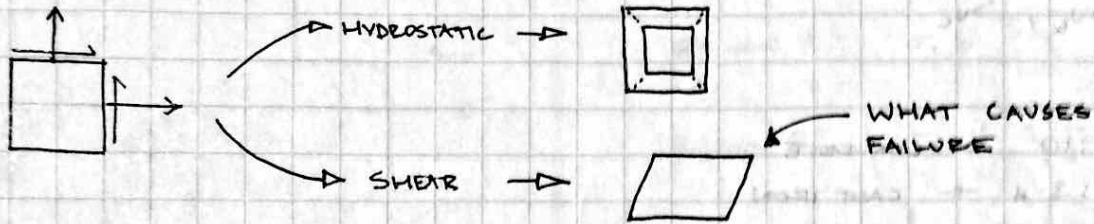


$$\tau_{MAX} = \frac{S_y}{2 \cdot F.S.} \rightarrow F.S. = \frac{S_y}{2 \cdot \tau_{MAX}}$$

$$F.S. = 1.5$$

1/22/2013

* DISTORTION ENERGY THEORY (VON-MISES, OCTAHEDRAL)



$$\sigma_{HYDRO} = \frac{1}{3}(\sigma_1 + \sigma_2 + \sigma_3)$$

$$\sigma_{DISTORION} = \frac{1}{\sqrt{3}} \left((\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_1 - \sigma_3)^2 \right)^{1/2}$$

* FAILURE PREDICTED TO OCCUR WHEN $\sigma_{DIS} \geq \frac{S_y}{F.S.}$ *

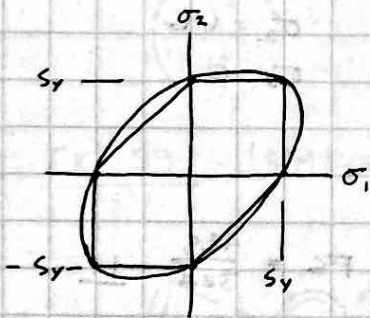
- UNIAXIAL CONDITION:

$$\sigma_2 = \sigma_3 = 0 \Rightarrow \sigma_{DIS} = \frac{1}{\sqrt{3}} (S_y^2 + S_y^2)^{1/2} = \frac{\sqrt{2}}{3} S_y$$

$$= \frac{1}{\sqrt{2}} \left((\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_1 - \sigma_3)^2 \right)^{1/2}$$

- FOR PLANE STRESS:

$$\left(\sigma_1^2 - \sigma_1 \sigma_2 + \sigma_2^2 \right)^{1/2} \geq \frac{S_y}{F.S.} \quad \text{OR} \quad \left(\sigma_x^2 - \sigma_x \sigma_y + \sigma_y^2 + 3\tau_{xy}^2 \right)^{1/2} \geq \frac{S_y}{F.S.}$$



FOR EXAMPLE:

$$\frac{1}{\sqrt{2}} \left(38.4^2 + 6.6^2 + (38.4 - 6.6)^2 \right)^{1/2} \geq \frac{S_y}{F.S.}$$

F.S. = 1.6

* MAX SHEAR IS MORE CONSERVATIVE THAN DISTORTION ENERGY

* QUIZ ON THURSDAY

- FAILURE THEORIES PRESENT TODAY (NOTES ALLOWED)
- STRESS AT A POINT
- EQUILLIBRIUM.

1/24/2013

* BRITTLE FAILURE THEORIES

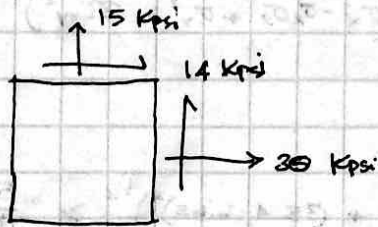
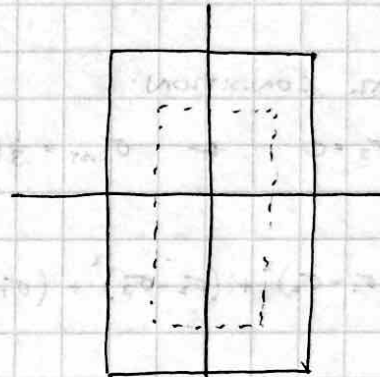
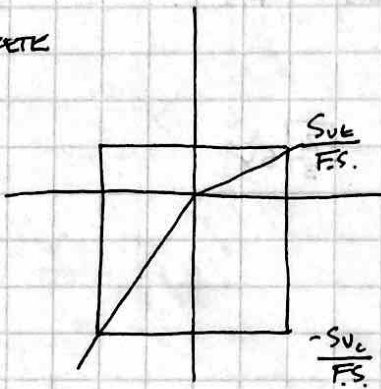
S_{ue} , S_{uc}

1:10 \rightarrow CONCRETE

1:3-4 \rightarrow CAST IRON

- MAXIMUM NORMAL

CONCRETE



ASTM A0

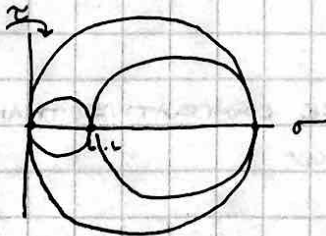
$S_{ub} = 42.5$ Kpsi

$S_{uc} = 140$ Kpsi

$\sigma_1 = 38.4$

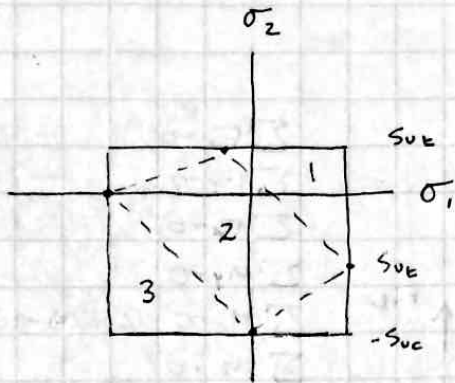
$\sigma_2 = 6.6$

$\sigma_3 = 0$



$$\sigma_1 = \frac{S_{ub}}{F_s} \rightarrow F_s = \frac{42.5}{38.4} = 1.1$$

1/24/2013



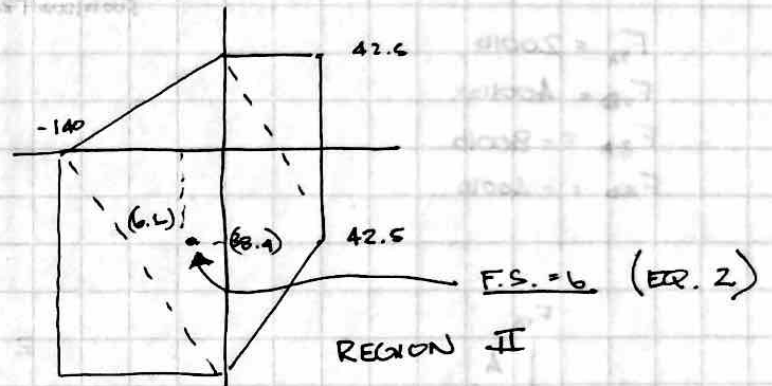
MODIFIED MOHR THEORY:

REGION 1: $\sigma_1 \geq \frac{S_{uc}}{F.S.}$

REGION 3: $\sigma_3 \leq \frac{-S_{uc}}{F.S.}$

REGION 2: $\frac{1}{F.S.} = \sigma_1 \left(\frac{S_{uc} - S_{uc}}{S_{uc} S_{uc}} \right) - \frac{\sigma_3}{S_{uc}}$

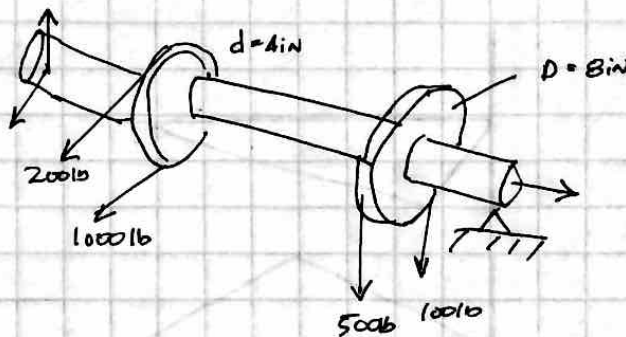
$\sigma_x = -30$ $\sigma_1 = 0$
 $\sigma_y = -15$ $\sigma_2 = -6.6$
 $\tau_{xy} = 14$ $\sigma_3 = -38.4$



1/29/2013:



EX. 39 (SIMILAR TO ~~THE~~ PROBLEM ON EXAM)

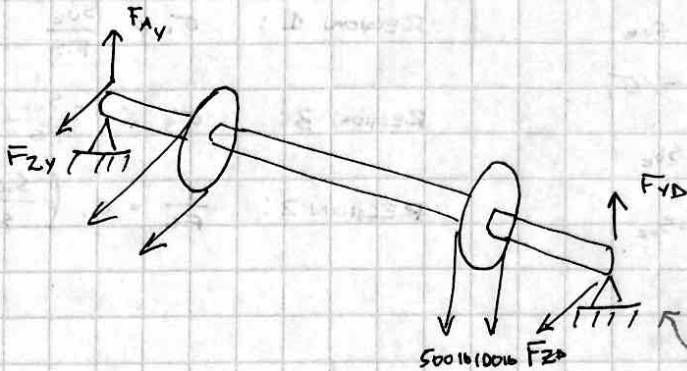


A.) $S_y = 81$ Kpsi
F.S. = ?

B.) CAST IRON
 $S_{ur} = 30$ Kpsi
 $S_{uc} = 100$ Kpsi

1/29/2018

EX. 3.9 CONT.



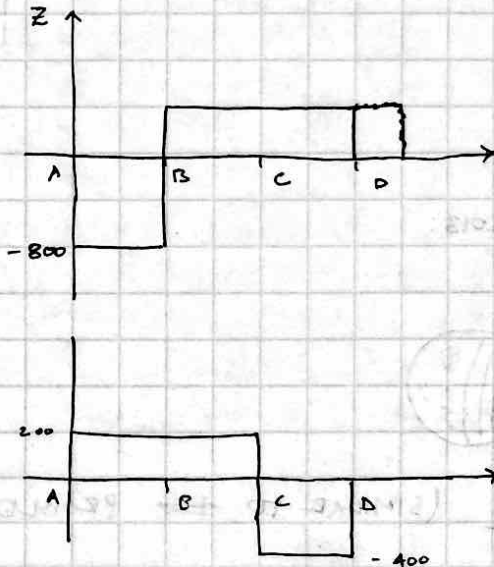
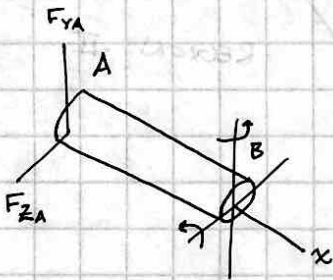
$$\begin{aligned} \sum F_x &= 0; \\ \sum F_y &= 0; \\ \sum F_z &= 0; \\ \sum M_y &= 0 \\ \sum M_x &= 0 \quad (200)(6) - (1000)(6) + (500)(4) - (100)(4) \\ \sum M_z &= 0 \end{aligned}$$

$$\begin{aligned} F_{yA} &= 200 \text{ lb} \\ F_{yB} &= 400 \text{ lb} \\ F_{zA} &= -800 \text{ lb} \\ F_{zB} &= -400 \text{ lb} \end{aligned}$$

WORK PROBLEM WITHOUT THIS SUPPORT FOR TEST

* ASSUMPTIONS:

- NO EXTERNAL FORCES CAUSING FORCES IN X-DIR. SO $\sum F_x = 0$



$$M_B = \sqrt{8000^2 + 2000^2} = 8250 \text{ in-lb}$$

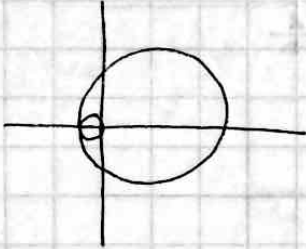
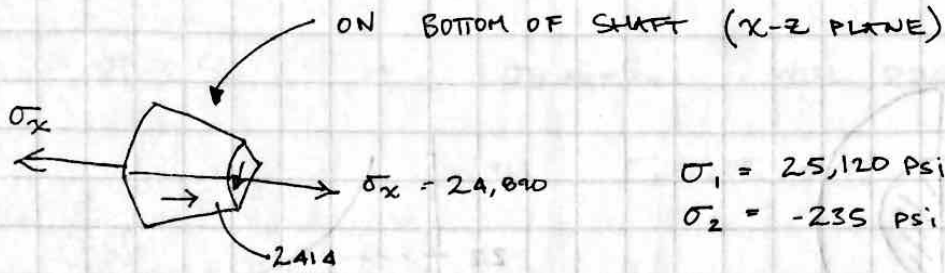
$$M_C = 5600 \text{ in-lb}$$

$$\tau_{TB} = \frac{T r}{J} = 2414 \text{ psi}$$

$$\sigma = \frac{M_C}{I} = 24890 \text{ psi}$$

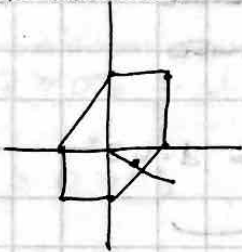
$$\tau_{BEND} = 603 \text{ psi (TRANSVERSE)}$$

1/29/2013



APPLY A FAILURE THEORY

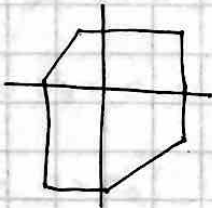
-FOR DUCTILE:



$$F.S. = 3.2$$

$$= \frac{81,000}{25,120} = 3.2$$

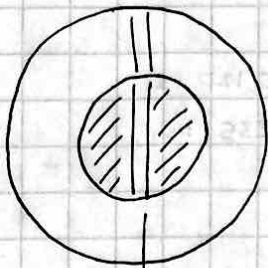
-FOR BRITTLE:



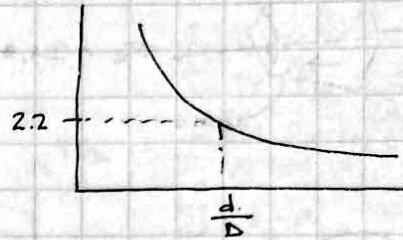
$$F.S. = 1.2$$

1/29/2013

* NEW MATERIAL: STRESS CONCENTRATIONS

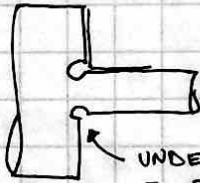


$d_{pin} = 0.15 in$
 $d_{shaft} = 1.5 in$



$K_t = 2.2$

$\sigma_{BENDING} * K_t$



UNDERCUT
TO RELIEVE
STRESS
CONCENTRATIONS

* FIND DIAMETER TO RAISE F.S. TO 3.2 AFTER K APPLIED

$$\frac{30000}{3.2 * K_t} = \frac{24890^{d/2}}{\frac{\pi}{64} d^4} \rightarrow d = 6.3''$$

CHANGES ITERATIVELY

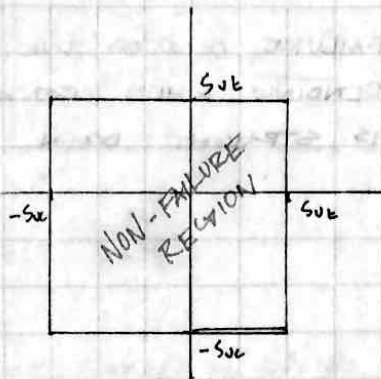
* READ FATIGUE

* READING NOTES: FAILURE THEORY - BRITTLE MATERIALS

- MAXIMUM NORMAL:

$\sigma_1 \geq S_{ut}$ OR $\sigma_3 \leq -S_{uc}$ WILL PREDICT FAILURE

WITH $\sigma_1 \geq \sigma_2 \geq \sigma_3$



DESIGN EQUATIONS:

$$\sigma_A = \frac{S_{ut}}{n}$$

$$\sigma_B = -\frac{S_{uc}}{n}$$

- BRITTLE-COULOMB-MOHR:

3 CASES:

$\sigma_A \geq \sigma_B \geq 0$	\rightarrow	$\sigma_A = \frac{S_{ut}}{n}$
$\sigma_A \geq 0 \geq \sigma_B$	\rightarrow	$\frac{\sigma_A}{S_{ut}} - \frac{\sigma_B}{S_{uc}} = \frac{1}{n}$
$0 \geq \sigma_A \geq \sigma_B$	\rightarrow	$\sigma_B = -\frac{S_{uc}}{n}$

- MODIFIED-MOHR:

$\sigma_A \geq \sigma_B \geq 0 \rightarrow \sigma_A = \frac{S_{ut}}{n}$

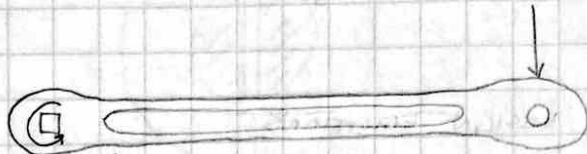
$\sigma_A \geq 0 \geq \sigma_B \rightarrow$

* 1/31/2013

- CHAPTER 6 SPREAD OUT TO 2 WEEKS

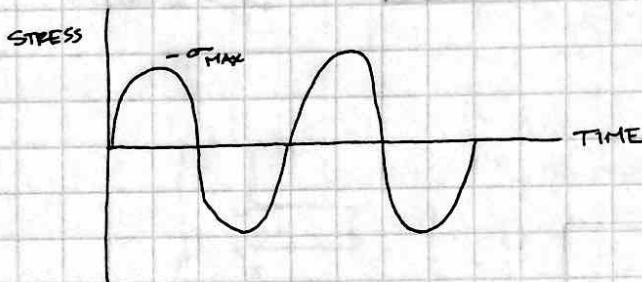
* CHAPTER 6 IS HARDEST CHAPTER *

- KNOW WELL

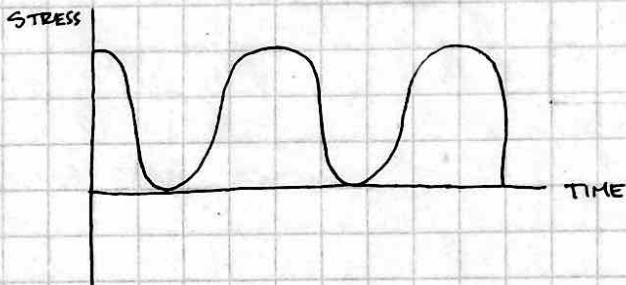


MAX. BENDING STRESS
w/ REDUCED AREA

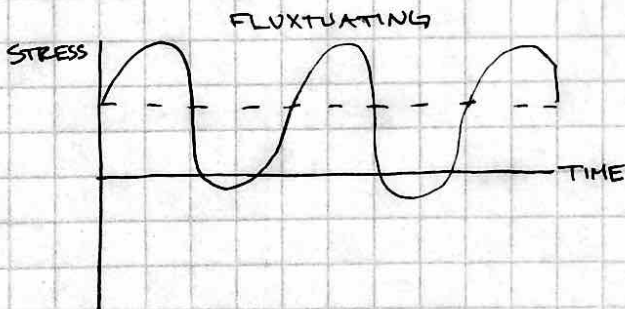
FAILURE OCCURED DUE TO
BENDING WHEN CRANK ARM
IS STRAIGHT DOWN.



FULLY - REVERSED



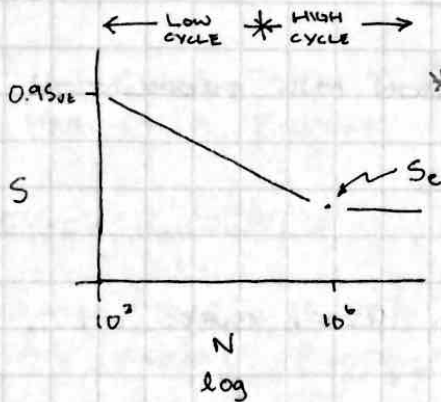
UNI-DIRECTIONAL
RELEASED



FLUCTUATING

1/31/2013:

* ENDURANCE LIMIT: STRESS FOR INFINITE LIFE, NOT ALL METALS POSSESS ONE



$$S_e' = 0.504 S_e$$

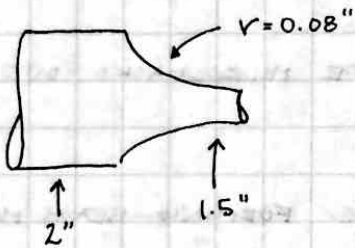
$$S_e = S_e' K_a K_b K_c K_d K_f$$

NOT ON EXAM!

- FAILURE IS PREDICTED TO OCCUR (UNIAXIAL LOADING, FULLY REVERSED, INFINITE LIFE) WHEN:

- SURFACE CORRECTION FACTOR

$$\frac{\sigma}{K_f} =$$



$$S_{UE} = 100$$

$$S_y = 84$$

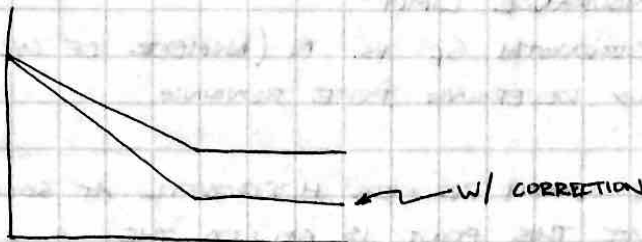
$$S_{surf} K_a = a S_{UE}^b = K_a = 0.785$$

$$S_{size} K_b = \left(\frac{d}{0.3}\right)^{-0.107} = K_b = 0.84$$

LOAD K_c

RELIABILITY FACTOR USUALLY INCLUDED IN

W/ CORRECTION:



* CHAPTER 6 READING NOTES:

- **FATIGUE FAILURE:** FAILURE DUE TO STRESS BEING LOADED REPEATEDLY A LARGE NUMBER OF TIMES

FATIGUE FAILURE IS DUE TO CRACK FORMATION AND PROPAGATION, AND IS INFLUENCED BY:

- RAPID CHANGES IN X-SECTIONAL AREA'S
- ELEMENTS THAT ROLL OR SLIDE
- COMPOSITION OF MATERIAL ITSELF
- CARELESSNESS OF LOCATION OF STAMP MARKS, BURRS, ETC...
- TEMPERATURE
- CORROSIVE ENVIRONMENT

CRACKS WILL GROW ALONG PLANES NORMAL TO THE MAXIMUM TENSILE STRESS

- **STAGES OF FATIGUE FAILURE:**

- **STAGE 1:** INITIATION OF ONE OR MORE MICROCRACKS DUE TO PLASTIC DEFORMATION.
- **STAGE 2:** MICROCRACKS \rightarrow MACROCRACKS FORMING BEACH MARKS
- **STAGE 3:** OCCURS DURING FINAL STRESS CYCLE WHEN REMAINING MATERIAL CANNOT SUPPORT LOAD. RESULTS IN SUDDEN FAST, FRACTURE.

METHODS FOR ANALYZING FATIGUE FAILURE IN ANALYSIS AND DESIGN:

- **FATIGUE STRENGTH AND ENDURANCE LIMIT**
 - GRAPH OF FATIGUE STRENGTH S_f VS. N (NUMBER OF CYCLES), LOADING IS SINUSOIDALLY REVERSING PURE BENDING.
 - FOR SOME MATERIALS, THE GRAPH BECOMES HORIZONTAL AT SOME POINT, THE STRENGTH AT THIS POINT IS CALLED THE ENDURANCE LIMIT.

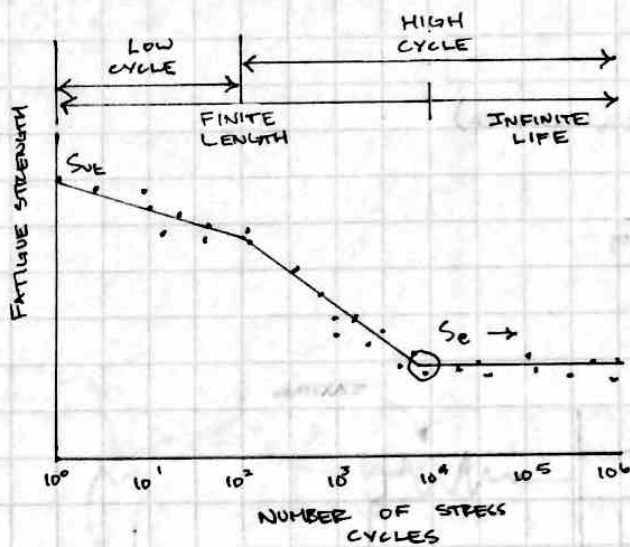
* 3 MAJOR FATIGUE LIFE METHODS:

- GOAL IS TO PREDICT WHEN (IN NUMBER OF CYCLES), A PART WILL FAIL UNDER A GIVEN LOADING.

- LOW-CYCLE FATIGUE (LESS THAN 10^3 CYCLES)
- HIGH-CYCLE FATIGUE (MORE THAN 10^3 CYCLES)

STRESS-LIFE METHOD:

VARYING AMOUNTS OF STRESS APPLIED TO MATERIAL IN ROTATION UNTIL FAILURE. PLOTTED ON A SEMILOG SCALE



* NON-FERROUS MATERIALS HAVE NO ENDURANCE LIMIT *

1 2/5/2013

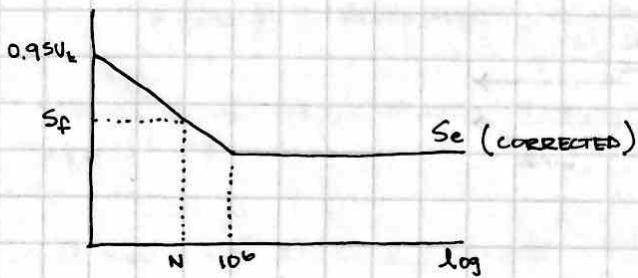
EXAM:

1 EQ.

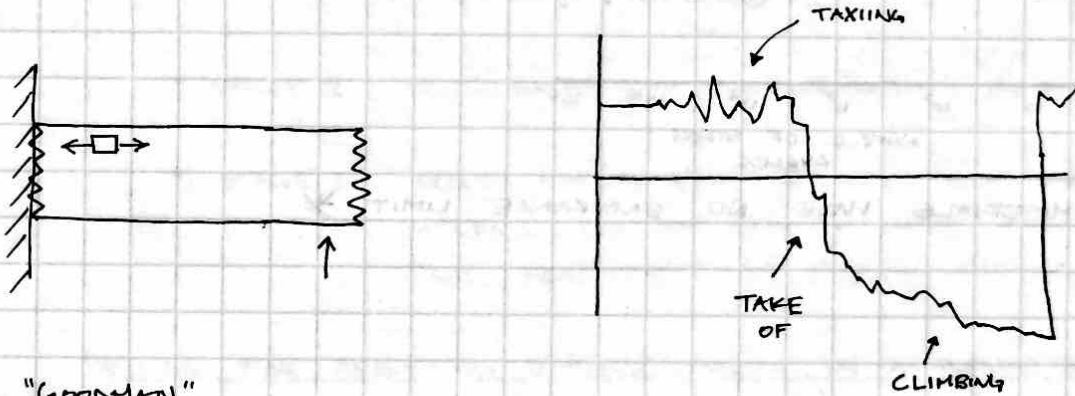
1 STRESS AT A POINT

1 WILL IT FAIL?

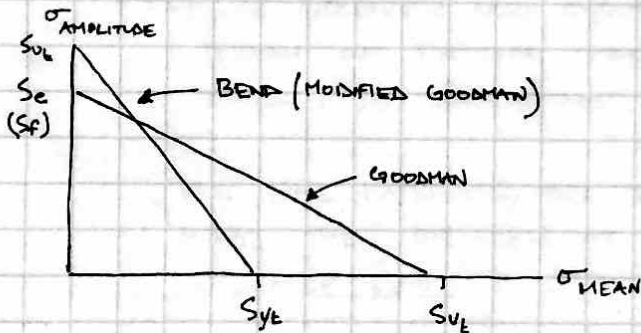
- 4 FAILURE THEORIES. 2 BRITTLE, 2 DUCTILE



AIR PLANE:



"GOODMAN"

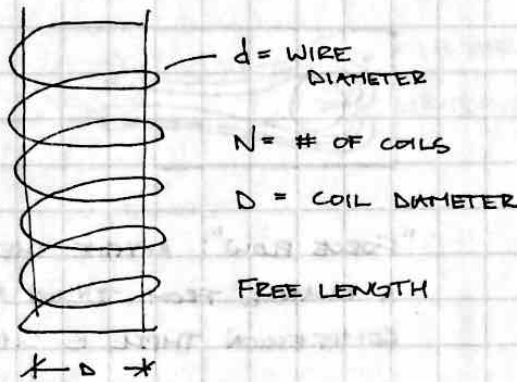


$$\frac{\sigma_A}{S_e} + \frac{\sigma_M}{S_u_e} = 1$$

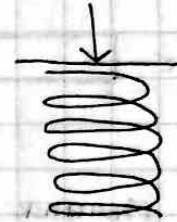
↳ F.S. GOES IN HERE

2/5/2013

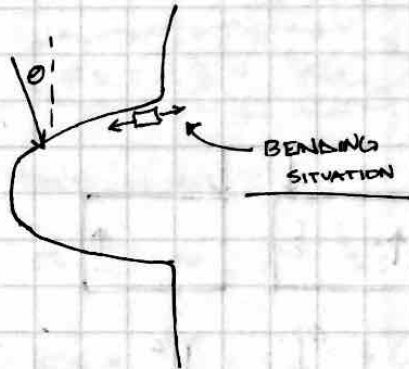
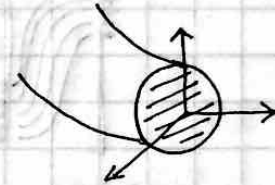
SPRINGS:



FBD



GEAR:



"ALMOST ANYTIME YOU HAVE ONE PART TOUCHING ANOTHER YOU HAVE A NORMAL FORCE"

2/12/2013

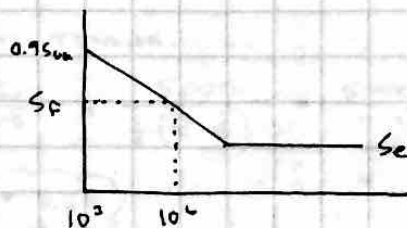
* ALL ASSIGNMENTS ON BB NOW *

- KNOW HOW TO DO ALL PROBLEMS ASSIGNED, LIKELY TO BE ON 2ND TEST.

* FATIGUE REVIEW:

$$S_e' = S_e K \dots$$

$$\frac{\sigma_w}{K_f} \gg \frac{S_e}{F.S.}$$

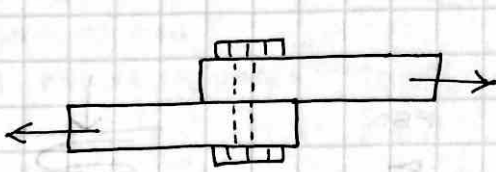


$$q = \frac{(0.95 S_u)^2}{S_e}, \quad b = -\frac{1}{3} \log \left(\frac{0.95 S_u}{S_e} \right)$$

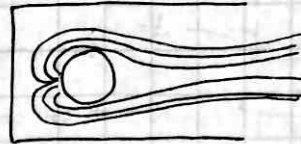
* ALL WILL BE ON EXAM *

2/12/2013

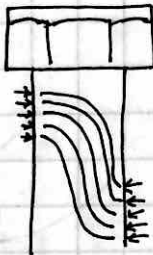
* FASTENERS



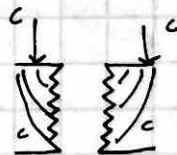
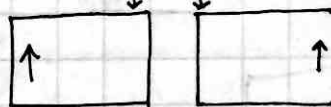
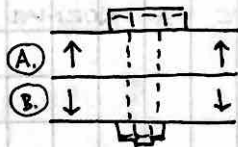
FASTENER IN SHEAR



"FORCE FLOW": ANYTIME THERE IS A CHANGE FROM TENSION TO COMPRESSION THERE IS SHEAR



FASTENER IN TENSION:



"WHAT'S THE FACTOR OF SAFETY?"

↳ TEST QUESTION

2/12/2013

EX. 8-67

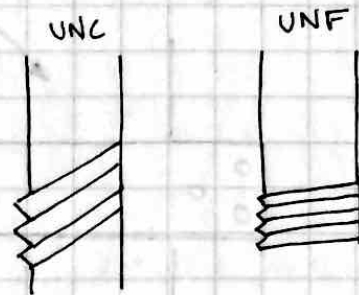
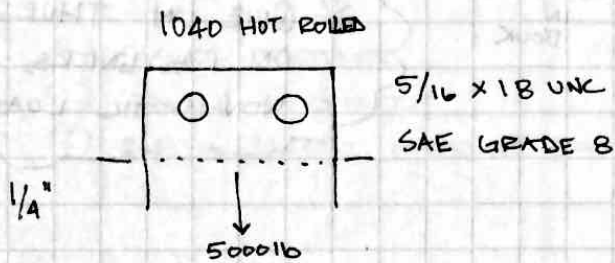


TABLE 8.6

$$S_y = 130 \text{ Kpsi}$$

$$S_{sy} = 0.577 S_y = 75 \text{ Kpsi}$$

SHEAR
YIELD

① BOLT SHEAR:

$$\tau \leq \frac{S_{sy}}{F.S.} \rightarrow F.S. = \frac{S_{sy}}{\tau} = \frac{5000}{2\pi \left(\frac{5}{16}\right)^2} = 32.6 \text{ Kpsi}$$

$$F.S. = 2.3 = \frac{75}{32.6}$$

② BOLT CRUSH:

$$\sigma = \frac{F}{A} \rightarrow \sigma \leq \frac{S_{yc}}{F.S.} \rightarrow \sigma = \frac{2500}{\left(\frac{\pi}{4}\right)\left(\frac{1}{4}\right)^2} = 32 \text{ Kpsi}$$

$$F.S. = \frac{S_{yc}}{\sigma} = \frac{130}{32} = 4.06$$

FASTENERS
RARELY
CRUSH

③ PARENT MATERIAL CRUSH:

$$F.S. = \frac{S_{yp}}{\sigma} =$$

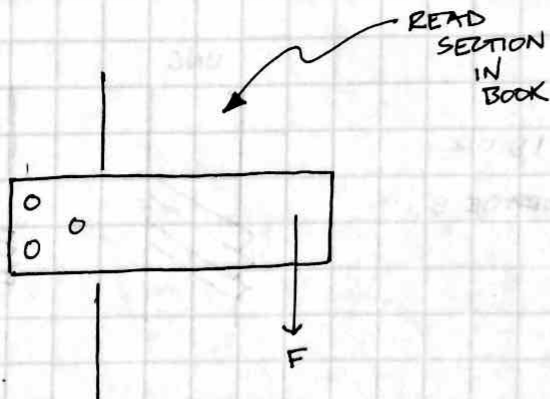
* EXPECT TO FAIL BY
PARENT CRUSH *

④ PARENT TENSION:

$$\sigma \leq \frac{S_y}{F.S.} = \frac{5000}{\frac{1}{4} \left(\frac{11}{8} - \frac{5}{8}\right)} = \frac{5000}{0.44} = 11.4 \text{ Kpsi}$$

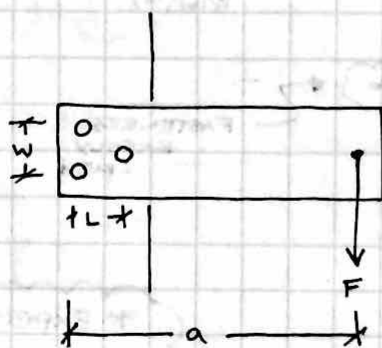
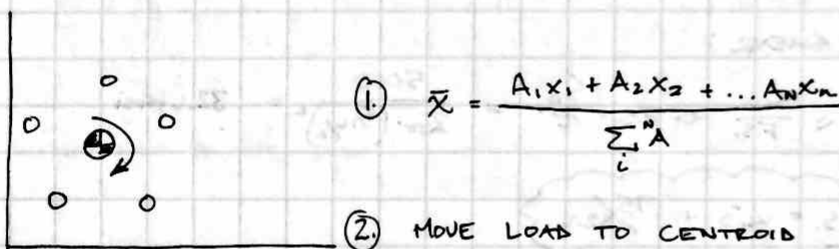
$$F.S. = 3.68$$

2/13/2013



* QUIZ ON THURSDAY ON FASTENERS, POSS. NON-STATIC LOAD *

2/14/2013

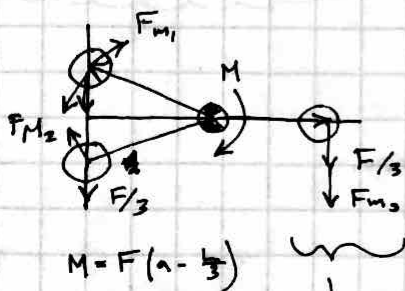


$$\bar{x} = \frac{A_1(0) + A_2(0) + A_3(L)}{A_1 + A_2 + A_3}$$

$$= \frac{L}{3}$$

$$\bar{y} = \bar{y} = \frac{A_1 \frac{h}{2} - A_2 \frac{h}{2} + A_3(0)}{A_1 + A_2 + A_3}$$

$$= 0$$



$$M = F_{m1} r_1 + F_{m2} r_2 + F_{m3} r_3$$

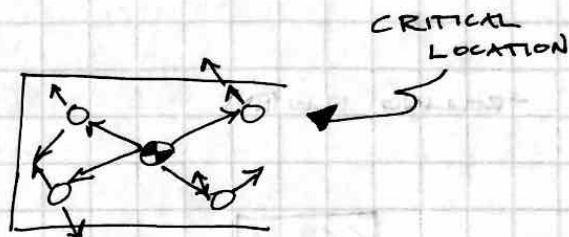
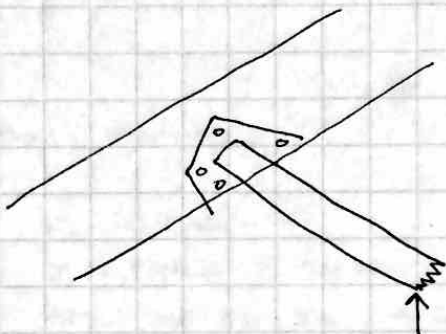
$$F_{m1} = \frac{M r_1}{\sum_i^n r_i^2}$$

CRITICAL FASTENER

2/14/2013

4. FOR MOST CRITICAL FASTENER, EVALUATE:

- ① SHEAR FASTENER
- ② CRUSH FASTENER
- ③ ~~SHEAR~~ PARENT MATERIAL CRUSH



* LOOK AT FASTENERS
IN TENSION *

* "WHEN IN DOUBT MAKE IT STOUT OUT OF THINGS YOU
KNOW ABOUT" *

* WEAR:

$$\frac{\delta}{t} = \frac{K}{H} * P * V$$

δ = WEAR

t = TIME (s)

K = WEAR COEFFICIENTS

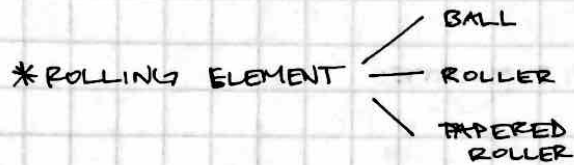
H = SURFACE HARDNESS

P = SURFACE PRESSURE

V = SLIDING VELOCITY

MICROSCOPIC SPOT WELDS
IN BETWEEN SURFACES

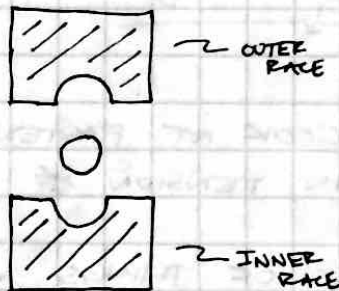
2/19/2013



* HYDRODYNAMIC

* SLIDING ELEMENT

- ROLLING ELEMENT

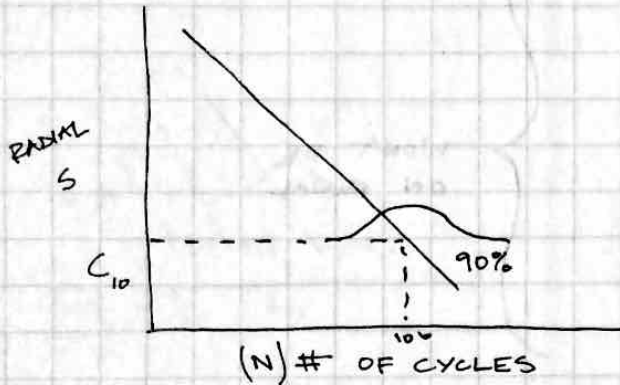


SINTERED BRONZE (SELF LUBRICATING)

TWO NUMBERS TO BE CONCERNED WITH

C_0	C_{10}
↑	↑
STATIC	DYNAMIC

2/21/2013



$$L = L_{10} \left(\frac{C_{10}}{F_e} \right)^a$$

$a = 3$ (BALL BEARING)

$a = \frac{10}{3} = 3.33$ (ROLLER)

$$L = \int h(b_0)$$

↑ hr ↑ rpm ↑ m/hr

BEARING EXAMPLE:

$$F_R = 5.5 \text{ KN}$$

$$\Sigma = 5000 \text{ H @ } 300 \text{ RPM}$$

SPEC AN O2 BB, 90% RELIABILITY

ANOTHER EXAMPLE

25mm bore, $F_R = 5500 \text{ N}$

- HOW LONG WILL IT LAST?

$$L = 10^6 \left(\frac{10,000}{5500} \right)^3 \rightarrow 16.5 \times 10^6 \text{ REV}$$

* RADIAL + AXIAL LOAD:

$$F_e = X V F_R + Y F_a$$

↑
EQ. RADIAL
LOAD

↑
ROTATION

$V = 1$ (INNER RACE ROTATES)

$V = 1.2$ (OUTER RACE ROTATES)

① $\frac{F_a}{V F_r}$

② TABLE 11-1 → PICK INITIAL X & Y VALUES

③ COMPUTE $F_e = X V F_r + Y F_a$

④ FIND B LOAD FACTOR

2/20/2013

5. COMPUTE $F_c = F_e \cdot F$

6. PICK BERG. FROM 11.2

7. $\frac{F_a}{C_0}$

8. TABLE 11.1

WON'T BE
ON FINAL

EX.

$$F_a = 1.5 \text{ KN}$$

$$F_r = 1.2 \text{ KN}$$

40 hr/WEEK, 15 YEARS, 1800 RPM

90% RELIABILITY, BALL 02

$$L = 3.24 \times 10^9 \text{ REV}$$

- INNER RING ROTATES, $V = 1.0$

$$X = 0.56$$

$$Y = 1.63$$

$$F_c = 0.56 \times 1.2 + 1.63 \times 1.5 = 3.07$$

$$F_c' = 3.07 + 1.2$$

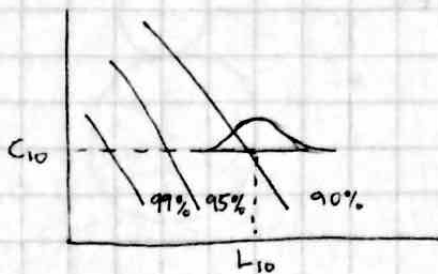
$$C_{10} = F_c' \left(\frac{L}{L_{10}} \right)^{1/3}$$

2/26/2013

$$C_{10} = F_{af} \left(\frac{x_D n_D 60}{x_R n_R 60} \right)^{1/4}, \quad L_{10} = L_R n_R 60 \left(\frac{C_{10}}{F_{af}} \right)^3$$

C_{10} x_0 , θ , b

2/26/2013



$$C_{10} = F_{AF} \left(\frac{x_D}{x_D + (\theta - x_D)(1 - R_D)^{1/b}} \right)^{1/a}$$

EX.

$F_D = 413 \text{ lb}$

$a_f = 1.2$

$L = 30,000 \text{ hr @ } 300 \text{ RPM}$

$R_D = 99\%$

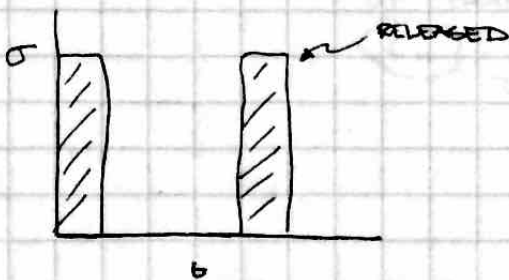
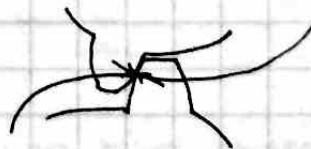
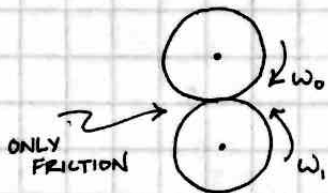
$\rightarrow L_D = 30000$

$L_D = 540 \times 10^6 \text{ REV}$

$x_D = 540 = \frac{540 \times 10^6}{1 \times 10^6} = \left(\frac{L_D}{L_{10}} \right)$

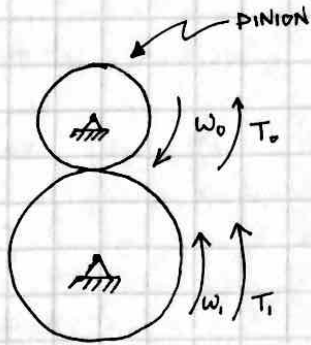
$= 413 \times 1.2 \left(\frac{540}{0.2 + (4.459 - 0.02)(1 - 0.99)^{1/1.487}} \right)^{1/3}$

* GEARS

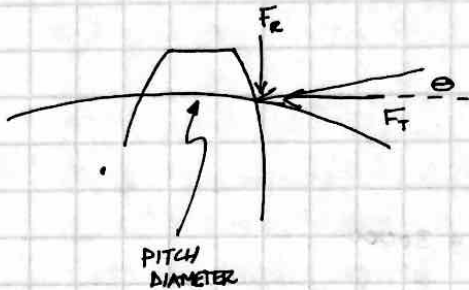


* IDELERS ARE FULLY REVERSED *

2/26/2013



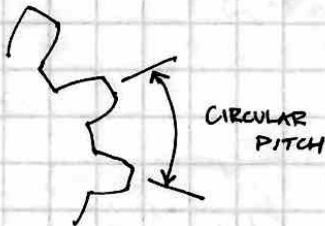
$$P = \omega T = Fv$$



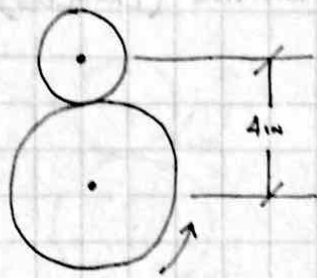
$$\omega_o = \omega_i \left(\frac{r_i}{r_o} \right)$$

$$\text{DIAMETRICAL PITCH } P = \frac{\# \text{ TEETH}}{\text{PITCH DIAM}}$$

$$\frac{r_i}{r_o} = \frac{dp_i}{dp_o} = \frac{N_i}{N_o} \rightarrow \omega_o = \omega_i \left(\frac{N_i}{N_o} \right)$$



2/26/2013



$$P = 6 \text{ in}$$

$$W_p = W_g \left(\frac{r_g}{r_p} \right)$$

$$r_g + r_p = 4, \quad r_p = 1$$
$$r_g = 3$$

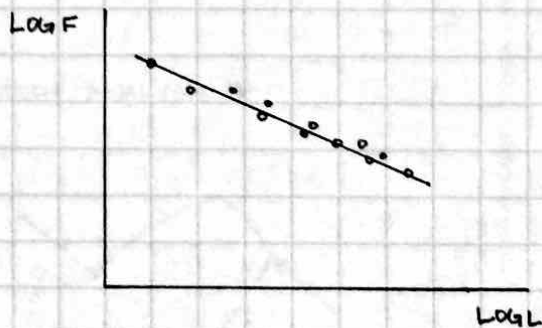
$$N_g = P r_g Z = 36$$

$$N_p = 12$$

* QUIZ ON 2 BEARING EQUATIONS

* READING NOTES: BEARINGS

- RATING LIFE: # OF REVOLUTIONS ^{OR HOURS} AT A CONSTANT SPEED THAT 90% WILL ACHIEVE OR EXCEED BEFORE FAILURE. REFERRED TO AS **L₁₀ LIFE**



$$FL^a = \text{CONST}$$

$$a = 3 \text{ FOR BS}$$

$$a = 10/3 \text{ FOR ROLLER}$$

- CATALOG LOAD: RADIAL LOAD THAT CAUSES 10% OF A GROUP OF BEARINGS TO FAIL. REFERRED TO AS

C₁₀ . OR BASIC DYNAMIC LOAD RATING.

→ REFERENCE VALUE (NOT USUALLY ACHIEVED BY THE BEARING)

2/27/2013

$$F_1 L_1^{1/a} = F_2 L_2^{1/a} \rightarrow \text{LOAD RATING (CATALOG)}$$

AND LIFE RATING INSERTED:

$$F_R L_R^{1/a} = F_D L_D^{1/a}$$

- R: RATED

- D: DESIRED

- LIFE EXPRESSED IN HOURS AT A GIVEN SPEED

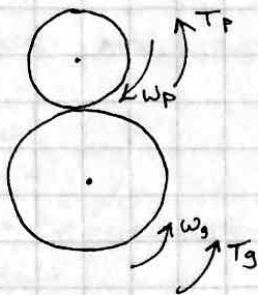
$$L = 60 \mathcal{L} n$$

\mathcal{L} = HOURS

n = REV/MIN

$$C_{10} = F_R = F_D \left(\frac{L_D}{L_R} \right)^{1/a} = F_D \left(\frac{\mathcal{L}_D n_D 60}{\mathcal{L}_R n_R 60} \right)^{1/a}$$

2/28/2013



$$\left. \begin{aligned} T_g &= r_g \omega_g \\ T_p &= r_p \omega_p \end{aligned} \right\}$$

$$\frac{T_g}{T_p} = \frac{r_g}{r_p} = \frac{N_g}{N_p}$$

OF TEETH

$$P_{in} = T_g \omega_g = \frac{T_p N_g}{N_p} \omega_p \frac{N_p}{N_g} = P_{out}$$

$$\eta = 0.98$$

$$P_{out} = \eta P_{in}$$



* EXAMPLE *

$$N_g = 30$$

$$N_p = 20$$

$$P = 6$$

$$T_p = 144 \text{ in}\cdot\text{lb}$$

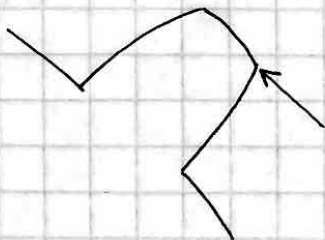
$$\omega_p = 1800 \text{ RPM}$$

$$T_g = ?$$

$$\omega_g = ?$$

$$HP = \frac{W E V}{33,300}$$

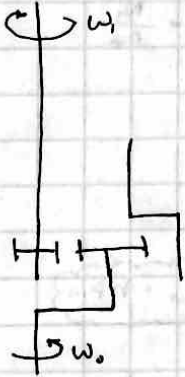
* GEAR TEETH ANALYSIS *



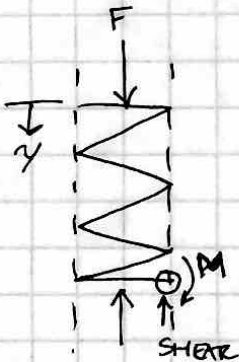
ASSUMPTIONS:

- LOAD AT TIP
- BEAM BENDING

$$\frac{N_r}{N_s} W_r = \left(1 + \frac{N_r}{N_s}\right) W_A - W_S$$



* KNOW STRESS STATES IN SPRINGS, BEVEL WASHERS *



$$\tau_{MAX} = K_s \frac{8FD}{\pi d^3}$$

$$K_s = \frac{2c+1}{2c}$$

$$y = \frac{8FD^3 N_a}{d^4 G} \quad \leftarrow \quad \# \text{ OF ACTIVE COILS}$$

SPEC SPRINGS:

- MIN WORKING LENGTH
- FREE LENGTH
- SOLID LENGTH
- $N_t * d$

3/12/2013

SPRINGS

* TABLES GIVEN ON EXAM *

N_T = SQUARED AND GROUND

$$N_A = 5$$

$$OD = 31.3 \text{ mm}$$

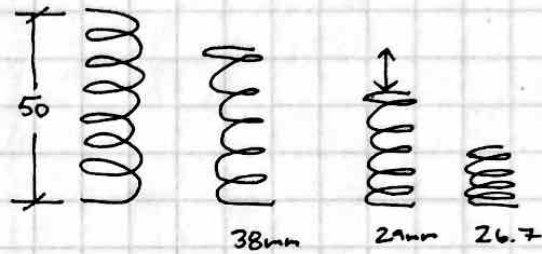
$$d = 3.82 \text{ mm}$$

$$L_0 = 50 \text{ mm} \leftarrow \text{FREELONGTH}$$

$$L_{MAX} = 38 \text{ mm}$$

$$L_{MIN} = 29 \text{ mm}$$

$$L_s = N_T d$$



$$K = \frac{d^4 G}{8D^3 N_A} = 20.3 \text{ kN/m} = 116 \text{ lb/m}$$

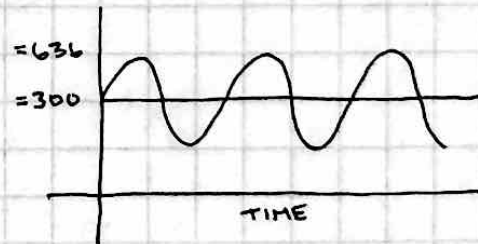
YIELD AT SOLID:

$$\tau_{MAX} = K \frac{8FD}{\pi d^3}$$

$$K_w, K_s = \frac{4c + 2}{4c - 3} = 1.19$$

$$\tau_{MAX} = 705 \text{ MPa}$$

$$FS = \frac{800}{705} = 1.13$$



* CHAPTER 14 * HELICAL AND SPUR GEARS *

BENDING STRESS IN GEARS → LEWIS BENDING EQUATION:

$$\sigma = \frac{Mc}{I} = \frac{6W\ell}{F\ell^2}$$